

# Semantic Processing

### The Lexer and Parser...

- Found lexical and syntax errors
- Built Abstract Syntax Tree

### Now...

- Find semantic errors.
- Build information about the program.

### Later...

- Generate IR Code
- Optimize IR Code
- Generate Target Code

## Semantics - Part 1

### Semantic Errors

#### Undefined ID / ID is already defined

Other name-related checks (e.g., can't redefine "true")

Field labels

Labels on loops, gotos, etc.

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Wrong number of arguments

Type of arguments

Void / non-void conflict

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#### OOP-related checks

Does this class understand this message?

Is this field in this class?

Is private / public access followed?

## Semantics - Part 1

### “Blocks”

Contain variables

May be nested

May contain variable declarations

```
{  var x,y: int;
  ...
  {  var x: double;
    ...
  }
  ...
}
```

#### Blocks in C++ and Java:

```
void foo {
  double x;
  ...
  for (int x = 0; ...) {
    ...
  }
  ...
}
```

#### Declarations of Variables

Apply to the statements in the block

...and statements in nested blocks

...unless “hidden” by other declarations

#### PCAT

Each “body” is a block

Outermost (main) block (at level 0)

Each procedure constitutes a new block

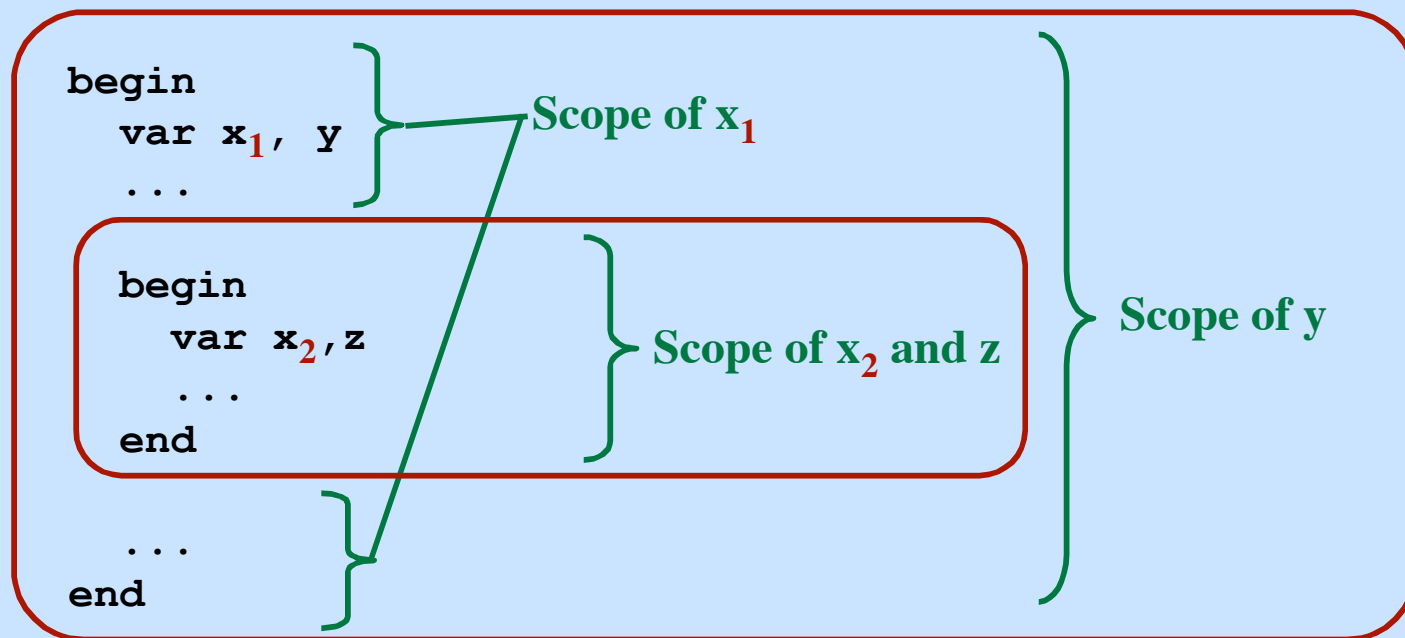
## Semantics - Part 1

### Scope

(Also: “**Lexical scope of variables**”)

Where is the variable visible? The scope of the variable.

**Scope rules** are given in the language definition.





## Semantics - Part 1

### Variations

*“Variable X’s scope extends from the beginning of the block in which it was declared, through the end of the block.”*

*“Variable X’s scope extends from the point of its declaration through the end of the block.”*

*“... Unless hidden by a new declaration of a variable with the same name!”*

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### PCAT

#### Variables

Visible (i.e., usable) only after their declaration.

#### Types, Procedures

Visible from the beginning of the block (to allow recursion).

PASS 1: Enter ID’s into symbol table

PASS 2: Check all uses

## Semantics - Part 1

```
var x,y,z                                     Level = 0
type T1,T2
procedure foo1 (x,a) is                       Level = 1
  var y,b
  type T2
  procedure foo2 () is
    var c                                     Level = 2
    begin
      ... ID ...
    end;
  begin
    ... ID ...
  end;
procedure foo3 () is                           Level = 1
  var
  begin
    ... ID ...
  end;
begin
  ... ID ... x ... foo1 ... a ... y ... foo2
end;
```

*“Static” Level*  
*“Lexical” Level*  
*(Textual)*

## Semantics - Part 1

### Functions as Data

```
var f,g: function;  
...  
f = function (a,b: Int) : Int is  
    var t: Int;  
    t = a*b;  
    return t-1;  
endFunction;  
...  
g = f;  
...  
i = g(7,5);
```

*This is like a constant.  
(It is an expression.)  
Within it is a new block.*

“Lambda Expressions”

“Closures”

“Nameless Functions”

***This idea is very powerful!***

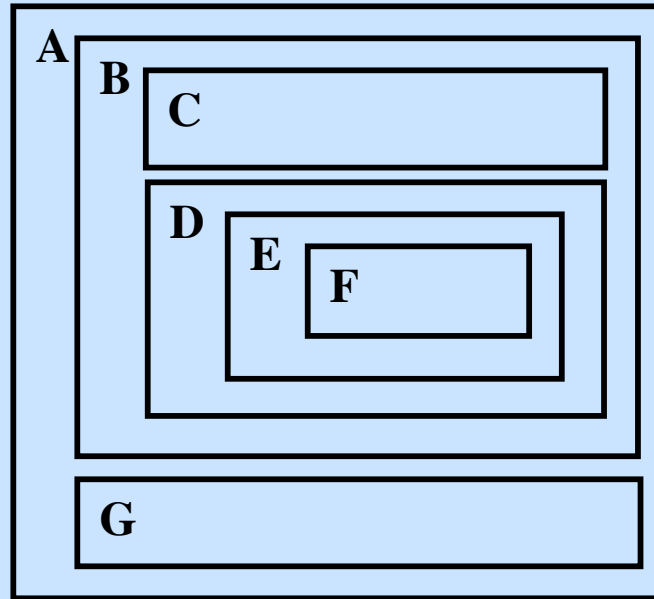
Programs may have more complex behavior

Programmers work at higher level of abstraction

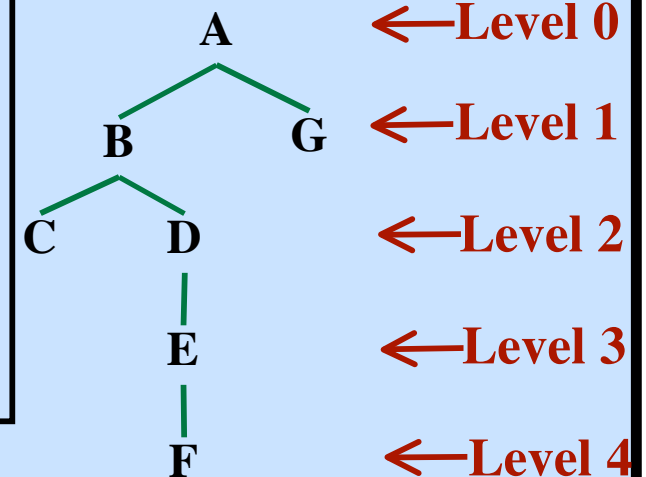
## Semantics - Part 1

### Blocks are Nested

```
begin A
  begin B
    begin C
    end
    begin D
      begin E
        begin F
        end
      end
    end
  end
  begin G
  end
end
```



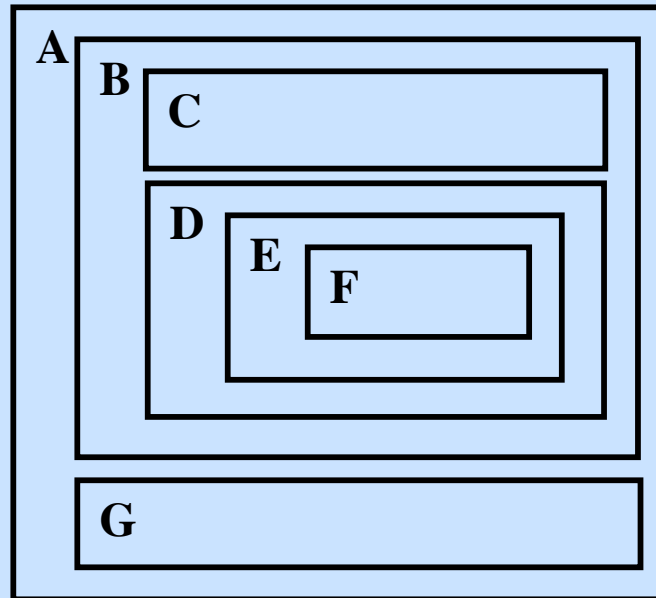
A sequential scan of the program will follow a depth-first traversal of this tree!



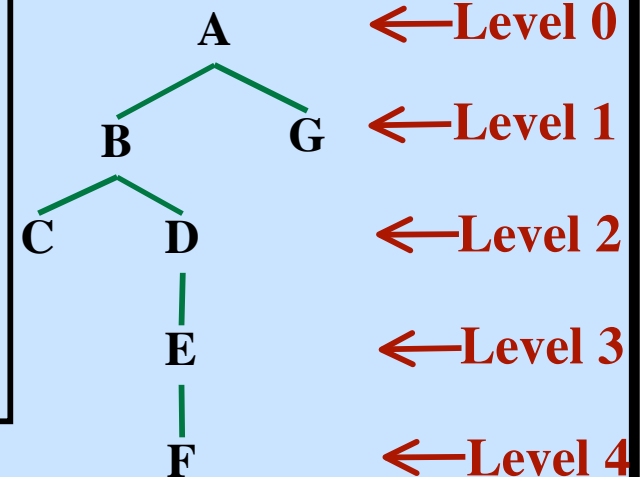
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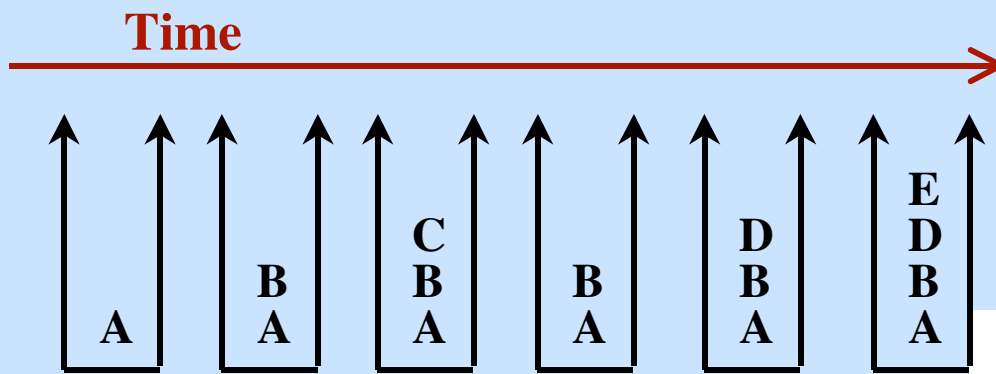


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*The symbol table will work like a stack*

openScope = **push**  
closeScope = **pop**



## Semantics - Part 1

### Goals of Type Checking

*Make sure the programmer uses data correctly.*

<code>x + y</code>	must have numeric types
<code>x = a;</code>	types must match (or be “compatible”)
<code>if (expr) then...</code>	type of expression must be boolean
<code>a[i]</code>	“a” must have type array, “i” must have type integer
<code>r.f</code>	“r” must have type record.
<code>foo (a,b,c)</code>	args must have the right types
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-------	---

*Determine how much space to allocate for each variable.*

Integer $\Rightarrow$ 32 bits
Double $\Rightarrow$ 64 bits
Char $\Rightarrow$ 8 bits
Boolean $\Rightarrow$ 1 bit

## Semantics - Part 1

### Types

Each language has its own notions of “type.”

Basic Types (also called “primitive types”)

`integer, real, character, boolean`

Constructed Types

Built from other types...

`array of ...`

`record { ... }`

`pointer to ...`

`function (...) → ...`

*Notations in other languages:*

```
int [100] a;
```

```
int *p;
```

```
int (* foo) (...) {...}
```

We must represent types within our compiler.

Might want a little language of “*type expressions*”.

To make explicit...

the universe of all possible types.

## Semantics - Part 1

### Basic Types

Each has a name

`integer`  
`real`  
`boolean`  
`char`  
`...`  
`void`  
`type_error`

*Close correspondence  
with keywords in  
the language*

Each basic type is a set of values.

Each type will have several  
Predefined operators on the values

#### Void

A type with zero values  
Used for typing functions

#### Type Error

Used to deal with semantic errors (not really a type)

## Semantics - Part 1

### Array Types

PCAT	<code>array of real</code>
Pascal	<code>array [1..10] of real</code>
C	<code>double x [10]</code>
Java	<code>double []</code>
Portlandish	<code>Array [Integer, Real]</code>

### Element Type (or “Base Type”)

Can be any type

Can even be other array type

```
array of array of real
a[i][j] = (a[i])[j]
```

### Index Type

Usually “integer”

...but other possibilities

```
Pascal: array [Days] of real
```

Often implicit, not really a part of the type

Is the size of the array part of the type???

## Semantics - Part 1

### Pointer Types

PCAT-style	<code>var p: ptr to integer;</code>
Pascal	<code>var p: ↑ integer;</code>
C	<code>int * p;</code>
Java	<code>MyRec p;</code>

### Element Type (or “Base Type”)

Can be any type.

### Typical Operations

Comparison	<code>==</code>
Copy	<code>=</code>
Dereference	<code>*p</code>
Increment	<code>p++</code>
Convert to/from integer	<code>p = (int *) 0x0045ff00;</code>

## Semantics - Part 1

### Record Types (“Structs”)

PCAT            var r: record  
                      value: real;  
                      count: integer;  
                      end;

C                struct {  
                      double value;  
                      int count;  
                      } r;

Java            class MyRec {  
                      double value;  
                      int count;  
                      }  
                      MyRec r;

Each record consists of several values of different types  
“components,” “fields”

Each component value has different type

The component values are identified by names (“field names”)

**r.value**

## Semantics - Part 1

### Product Types (Tuple Types)

Each tuple object consists of several component values.

Each component value has a different type.

(Similar to record types).

Component values are identified by position, not name.

To specify a product type:

#### Notation #1:

```
var t1: integer × boolean;  
      t2: real × real × real × real;
```

#### Notation #2:

```
var t1: (integer, boolean);  
      t2: (real, real, real, real);
```

To specify a tuple:

```
t1 = <6, true>;  
t1 = (6, true);  
t1 = [6, true];
```

To access the component values:

```
i = t1.1;           i = first(t1);  
x = t2.3;           x = third(t2);
```



## Semantics - Part 1

### List Types

Each list object consists of zero or more values, all with the same type.

To specify a list type:

#### Notation #1:

```
var myList: list of integer;
```

#### Notation #2:

```
var myList: List[integer];
```

To get the first element of the list:

```
i = head(myList);
```

```
i = car(myList);
```

To get a new list of everything else:

```
otherList = tail(myList);
```

```
i = cdr(myList);
```

Add an element to the front and create a new list:

```
newList = cons(i,myList)
```

```
newList = i.myList;
```

To create a list:

```
myList = [];
```

```
myList = [3,5,7];
```

```
myList = null;
```

```
myList = 3.5.7.null;
```

Other operations:

```
length, append, isEmpty
```

## Semantics - Part 1

### Function Types

Some languages include function types.

Need to associate types with function names.

Functions are “first-class” objects (e.g., they can be stored in arrays, etc.).

To specify a function type:

#### Notation #1:

*DomainType* → *RangeType*

```
var f: integer → boolean;
```

```
g: real × real × real × real → void;
```

#### Notation #2:

function (*DomainTypes*) returns *RangeType*

```
var f: function (integer) returns boolean;
```

```
g: function (real, real, real, real);
```

Operations:

#### Creation and Copy

```
f = function (a:int) returns boolean
```

```
...
```

```
return ...;
```

```
endFunction
```

Application/Invocation g (1.5, 2.5, 3.5, 4.5);

Comparison is usually not allowed.

## Semantics - Part 1

### Working with $\times$ and $\rightarrow$

Assumptions:

$\times$  is associative

$$\begin{aligned} & (\text{int} \times \text{int}) \times \text{int} \\ &= \text{int} \times (\text{int} \times \text{int}) \\ &= \text{int} \times \text{int} \times \text{int} \end{aligned}$$

$\times$  has greater precedence than  $\rightarrow$

$$\begin{aligned} & \text{int} \times \text{int} \rightarrow \text{int} \\ &= (\text{int} \times \text{int}) \rightarrow \text{int} \end{aligned}$$

$\rightarrow$  is right associative

$$\begin{aligned} & \text{int} \rightarrow \text{int} \rightarrow \text{int} \\ &= \text{int} \rightarrow (\text{int} \rightarrow \text{int}) \end{aligned}$$

## Semantics - Part 1

### Example

```
type Complex = real × real;
```

```
var c: Complex;
```

```
c = <1.2, 3.4>;
```

```
<x,y> = c;
```

```
function ComplexMult: Complex × Complex → Complex
```

```
    Complex × Complex → Complex  
    = (Complex × Complex) → Complex  
    = ((real × real) × (real × real)) → (real × real)  
    = real × real × real × real → real × real
```

```
<x,y> = ComplexMult (c, <5.6,7.8>);
```

## Semantics - Part 1

### Higher-Order Functions

```
function AddOne: real → real;  
AddOne = function (x:real) returns real  
    return x + 1.0;  
    endFunction;  
x = AddOne (123.0) ;  
x = AddOne (AddOne (AddOne (AddOne (AddOne (123.0) ) ) ) ) ) ;
```

Imagine a function which takes 2 arguments:

- A function, f
- An integer, N

It returns a function which...

when applied to argument x, will apply function f, N times.

```
function Repeat: (real → real) × int → (real → real) ;  
g = Repeat (AddOne, 5) ;           // g will add 5  
x = g (123.0) ;  
x = (Repeat (AddOne, 5)) (123.0) ;
```

Repeat is a “Higher-Order Function.”

*At least one argument or result is another function!*

## Semantics - Part 1

### A Syntax of Types

- T → int
- real
- bool
- char
- void
- TypeError
- array of T
- list of T
- ptr to T
- record ID : T { , ID : T }<sup>+</sup> endRecord
- T × T
- T → T
- ( T )

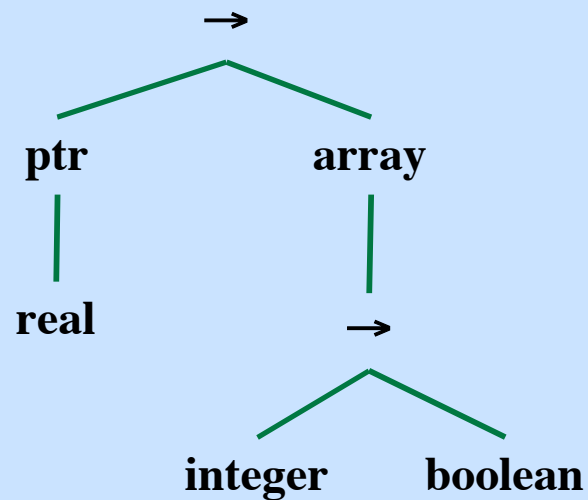
Represent each type with a tree  
An AST

## Semantics - Part 1

### Using Trees To Represent Types

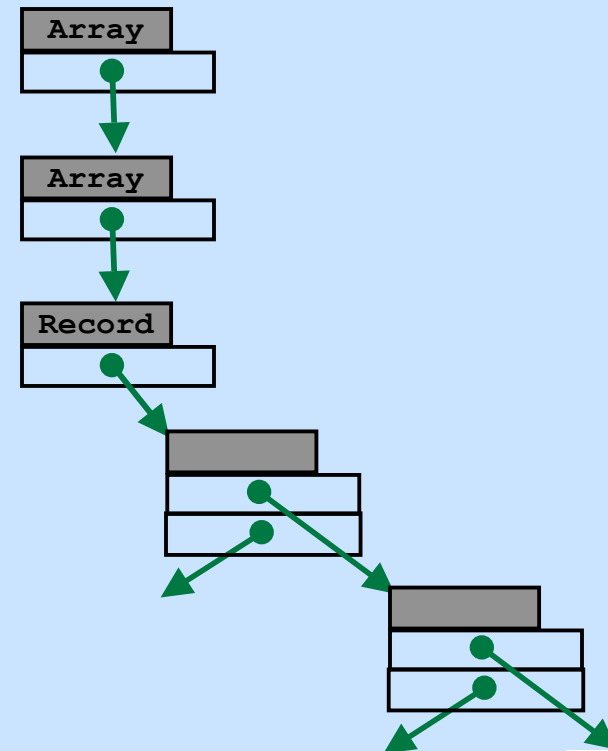
type T1 is (ptr to real) → (array of (integer → boolean));

The representation of T1...



In our PCAT compiler...

array of array of record ... end;



## Semantics - Part 1

### Naming Types

Associate a name with a type.

```
type MyRec is record ... end;
```

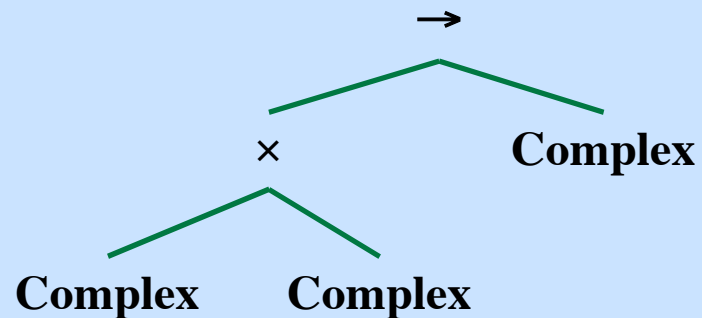
*name*                      *type*

Example:

```
type Complex is real × real;  
function ComplexMult (x, y: Complex) returns Complex is ...;
```

Or perhaps...

```
var ComplexMult: Complex × Complex → Complex;
```



Complex × Complex → Complex



# Semantics - Part 1

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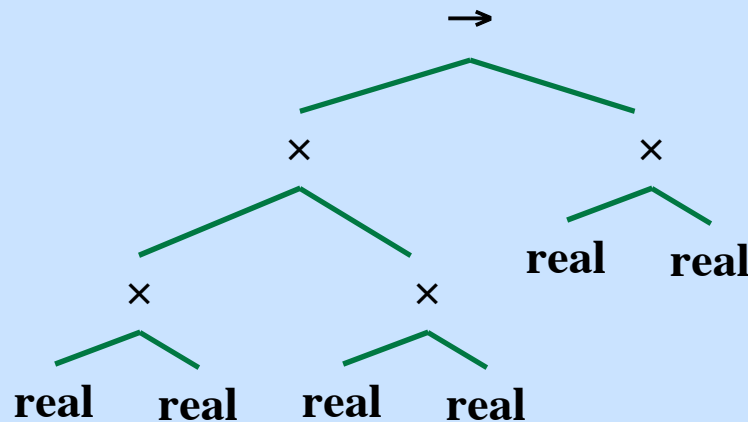
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*real × real × real × real → real × real*

### Static v. Dynamic Type Checking

#### “Static” Type Checking

Performed by the compiler

Errors detected?

Print a descriptive message and keep checking

Patch up the AST

Must cope with previous errors

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#### “Dynamic” Type Checking

Checking done at run-time

Compiler does not know about types.

```
var x, y, z;
```

```
...
```

```
x = y + z;
```

Each variable contains:

A value

Type information (“type tags”)

Examples:

Smalltalk / Squeak

Lisp

**Integer or Floating Addition?  
At runtime, do y and z contain  
integers or reals or ...?**

## Semantics - Part 1

### Untyped Languages

*Example:* Assembly Language

- There may be different types of data (integer, float, pointers, etc.)
- The programmer says which operations to use (iadd, fadd, ...)
- A type is not associated with each variable.
- If the programmer makes mistakes, the results are wrong.

## Semantics - Part 1

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### Strongly Typed Languages

- Each value has an associated type.
- Guarantees that no type-errors can happen.

*Example:*

```
x = "abc" ;  
y = "def" ;  
z = x - y ;
```

- C/C++

Type errors can occur, especially with casting.

“It is the programmer’s responsibility!”

**Error!**

**This operation cannot be  
done on this type of data.**

## Semantics - Part 1

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Type errors can occur, especially with casting.  
“It is the programmer’s responsibility!”

### Strong, Static Type Checking

- The compiler checks all types before runtime.
- No type-errors can occur.

*Examples:* Java, PCAT

### Types In PCAT

#### Basic Types:

int  
real  
bool  
string  
type\_of\_nil

#### Constructed Types:

array  
record

#### Other:

typeError

Representation of a type:

Pointer to the AST for the type

Type\_Error

We'll use "null" pointer

*The type rules for "nil"  
are different*

```
myArr := nil;  
myRec := nil;
```

### Approach To Static Type Checking

- *Need to describe types*

A representation of types

- *Associate a type with each variable.*

The variable declaration associates a type with a variable.  
This info is recorded (in the symbol table).

- *Associate a type with each expression*

...and each sub-expression.

- *Work bottom-up*

The type is a “synthesized” attribute

- *Check operators*

`expr1 + expr2`

Is the type of the expressions “integer” or “real”?

- *Check other places that expressions are used*

`LValue := Expr ;`

Is the type of “expr” equal to the type of the L-Value?

`if (expr) ...`

Is the type of the expression “boolean”?



### Operator Overloading

#### PCAT Example:

```
var x,y: int;  
...  
  x+y  
...
```

PCAT has two kinds of addition

The “+” operation is “*overloaded*”

Multiple meanings:

**iadd**

**fadd**

Also multiple kinds of negation, subtraction, multiplication, comparison, ...

Select correct operation based on argument types.

We’ll use the term “*mode*”

**INTEGER\_MODE**

**REAL\_MODE**

Tells which form of addition will be needed.

### Type Conversions

#### PCAT Example:

```
var i: int,  
    x: real;  
... (x + i) ...
```

Must convert the integer value to a real value first.

Real addition (**fadd**) will be used.

The result will be a real.

#### **Implicit Type Conversions (also called “Coercions”)**

- The language definition tells when they are needed.
- Compiler must insert special code to perform the operation.

#### **Explicit Type Conversions (also called “Casting”)**

```
... (i + (int) x) ...
```

- The programmer requests a specific conversion.
- The language definition tells when they allowed.
- The compiler may (or may not) need to insert special code.

## Semantics - Part 1

### Types In PCAT: Unary Operators

Given: Type of operand

Determine: Type of result

	<u>not</u>	+	-
int		int	int
real		real	real
bool	bool		
string			
array			
record			
type error			

Blank entries  
indicate "type error"

## Semantics - Part 1

### Types In PCAT: Unary Operators

Given: Type of operand

Determine: Type of result

#### *Implementation Ideas:*

7 × 3 array

```
ResultType[bool,not] => bool
```

Sequence of IF tests...

```
if (op == PLUS) or (op == MINUS) then  
  if typeOfOperand == int then  
    resultType = int;  
  elseif typeOfOperand == real then  
    resultType = real;  
  else  
    resultType = null; // TypeError;  
  endif  
elseif (op == NOT) then ...
```

	<u>not</u>	+	-
int		int	int
real		real	real
bool	bool		
string			
array			
record			
type error			

Blank entries  
indicate "type error"

## Semantics - Part 1

### Types In PCAT: Binary Operators

<u>Operand 1</u>	<u>Operand 2</u>	+ - *	/	and or	= <>	< <= > >=	div mod	:=
int	int	int	real*		bool	bool	int	ok
int	real	real*	real*		bool*	bool*		
real	int	real*	real*		bool*	bool*		ok*
real	real	real	real		bool	bool		ok
bool	bool			bool	bool			ok
type error	(any)							
(any)	type error							
(other)	(other)				bool**			ok**

\* means the int argument(s) must be coerced to real

\*\* means ok if the arguments are the same type

## Semantics - Part 1

### Types In PCAT: Binary Operators

<u>Operand 1</u>	<u>Operand 2</u>	+ - *	/	and or	= <>	< <= > >=	div mod	:=
int	int	int	real*		bool	bool	int	ok
int	real	real*	real*		bool*	bool*		
real	int	real*	real*		bool*	bool*		ok*
real	real	real	real		bool	bool		ok
bool	bool			bool	bool			ok
type error	(any)							
(any)	type error							
(other)	(other)				bool**			ok**

\* means the int argument(s) must be coerced to real

\*\* means ok if the arguments are the same type

#### *Implementation Ideas:*

Use a  $7 \times 7 \times 15$  array? Nah...

Switch on operator first, then on operand type.

### Recursive Types

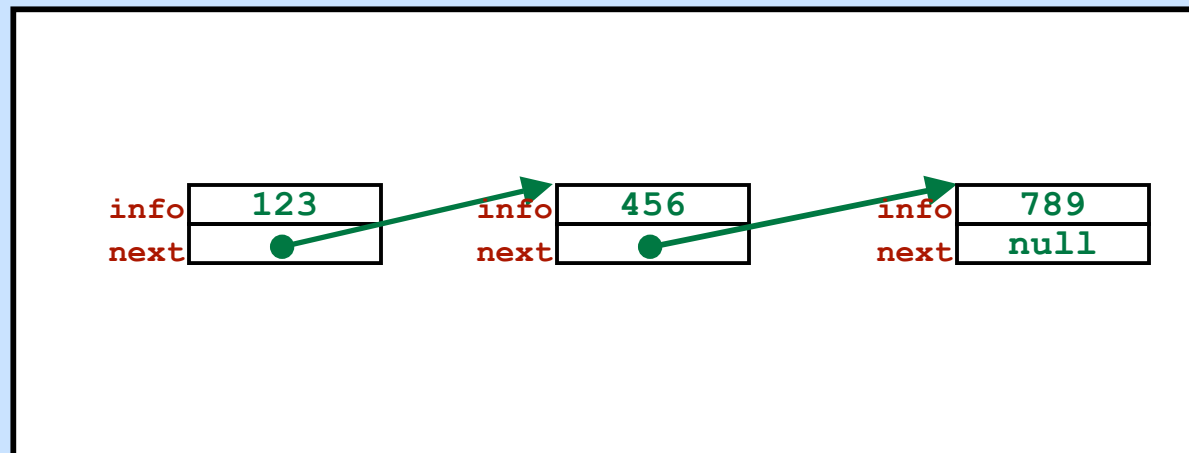
```
type MyRec is record  
    info: integer;  
    next: MyRec;  
    end;  
var x: MyRec := MyRec { info := 789;  
                        next := null };
```

## Semantics - Part 1

### Recursive Types

```
type MyRec is record  
    info: integer;  
    next: MyRec;  
end;  
var x: MyRec := MyRec { info := 789;  
                        next := null };
```

All records and arrays will go into the “Heap”.



The Heap

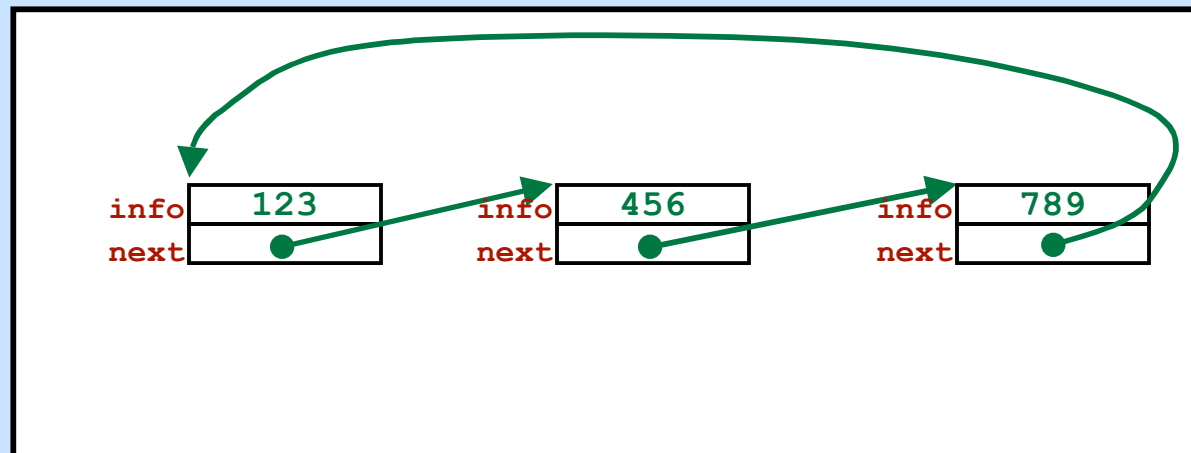


## Semantics - Part 1

### Recursive Types

```
type MyRec is record  
    info: integer;  
    next: MyRec;  
end;  
var x: MyRec := MyRec { info := 789;  
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All records and arrays will go into the **“Heap”**.



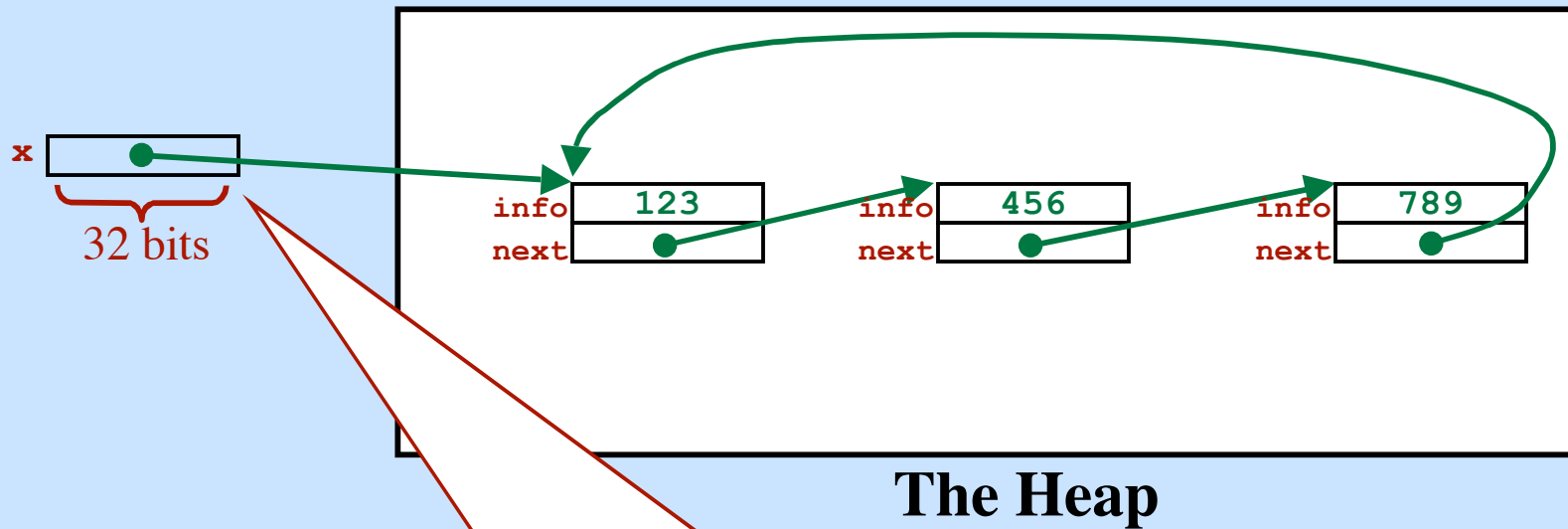
The Heap

# Semantics - Part 1

## Recursive Types

```
type MyRec is record  
    info: integer;  
    next: MyRec;  
end;  
var x: MyRec := MyRec { info := 789;  
                        next := null };
```

All records and arrays will go into the “Heap”.



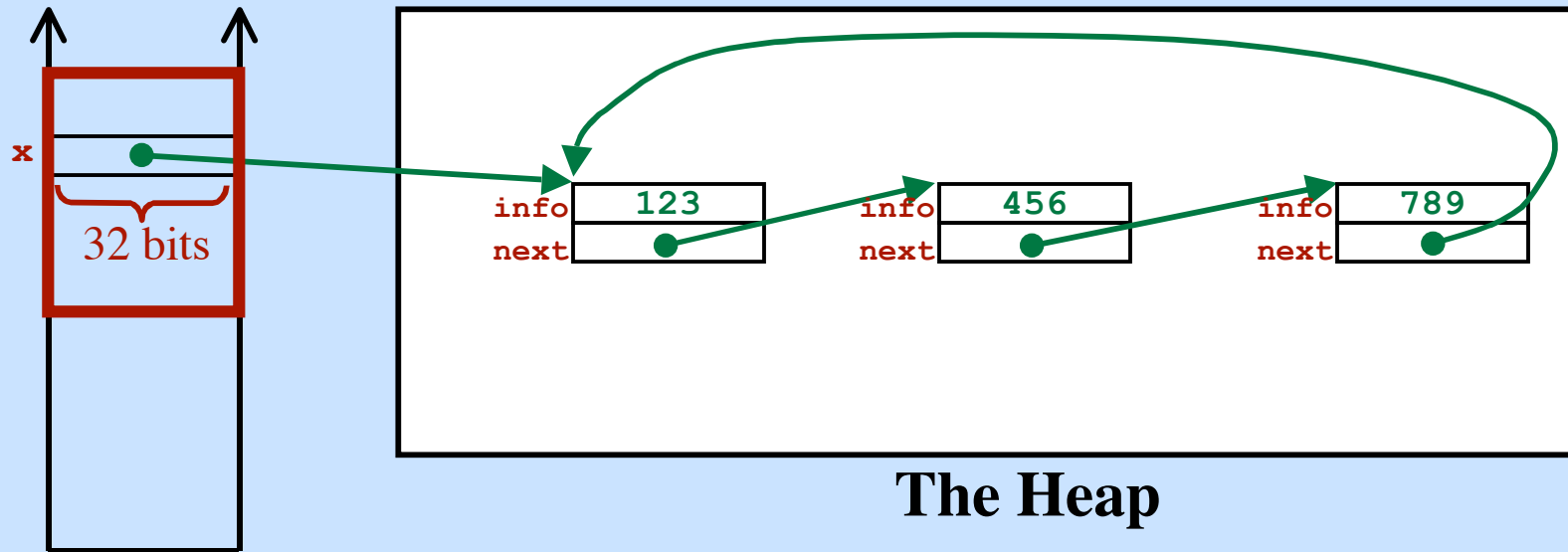
**Our Implementation: all variables will be 32 bits**

## Semantics - Part 1

### Recursive Types

```
type MyRec is record  
    info: integer;  
    next: MyRec;  
end;  
var x: MyRec := MyRec { info := 789;  
                        next := null };
```

All records and arrays will go into the “Heap”.



Runtime Stack of “Activation Records”  
 (“Stack Frames”)

The Heap

## Semantics - Part 1

### Type Equivalence

*What does it mean to say “type of operand 1” = “type of operand 2”?*

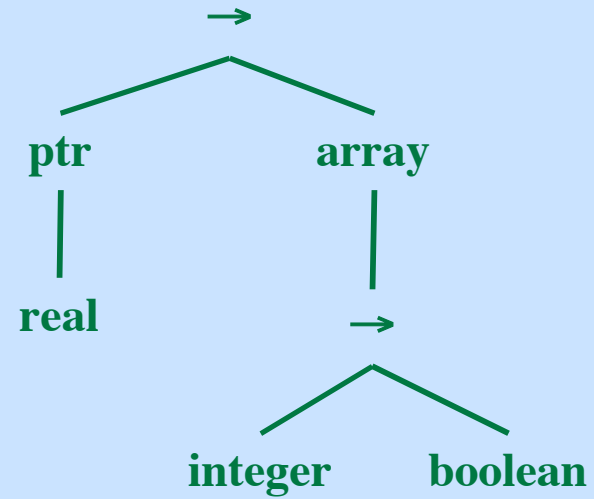
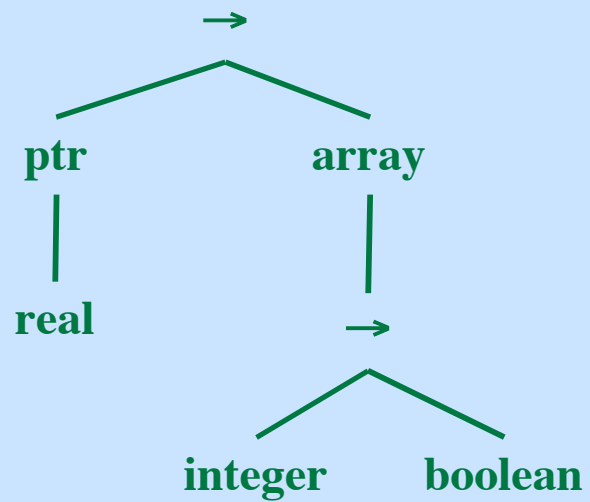
```
type T1 is record
    f: int;
    g: real;
end;
T2 is record
    f: int;
    g: real;
end;
T3 is T2;
var x: T1,
    y: T2,
    z: T3;
...
x := y;
```

Is the type of “x” the same as the type of “y”?

Is the type of “y” the same as the type of “z”?

## Semantics - Part 1

Types are represented as trees.

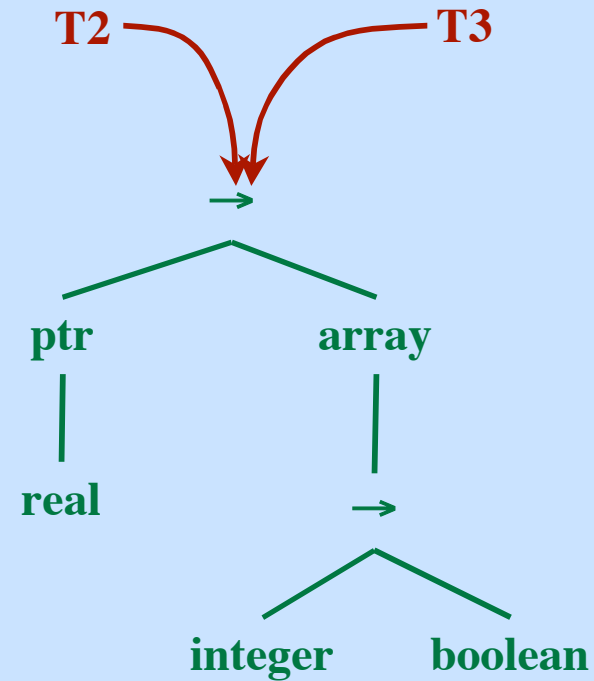
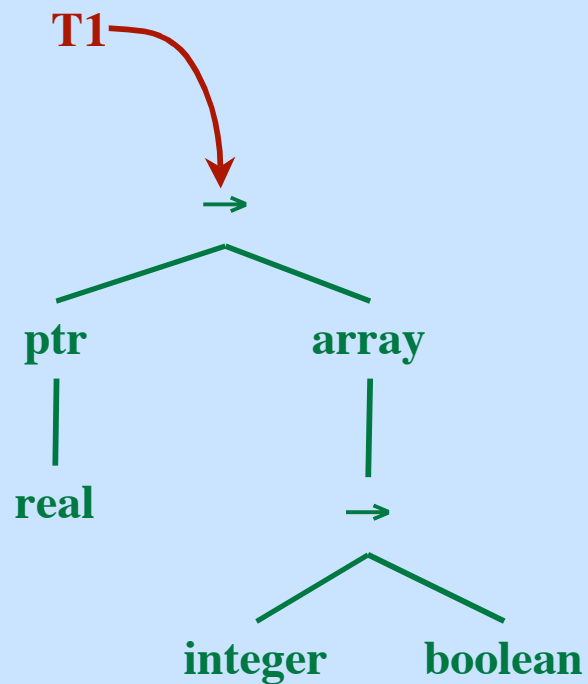


## Semantics - Part 1

Types are represented as trees.

Types may be named.

type T1 is ... ;



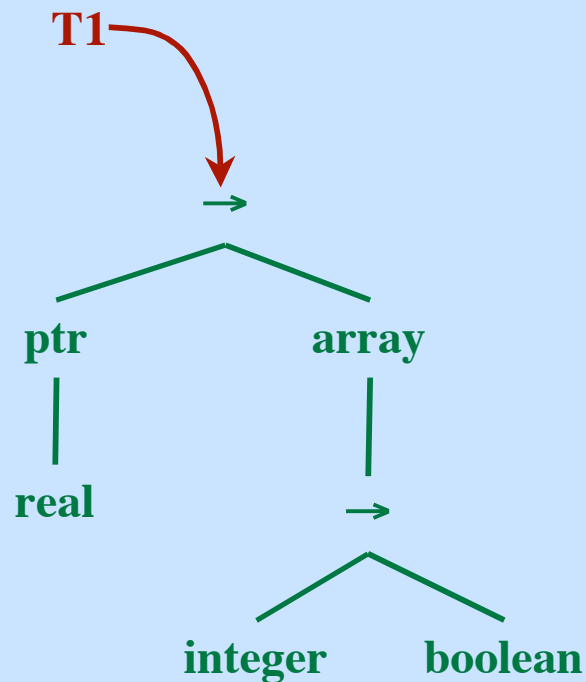
## Semantics - Part 1

### “Structural Equivalence”

Are the trees equivalent?

Isomorphic (same shape, same nodes)

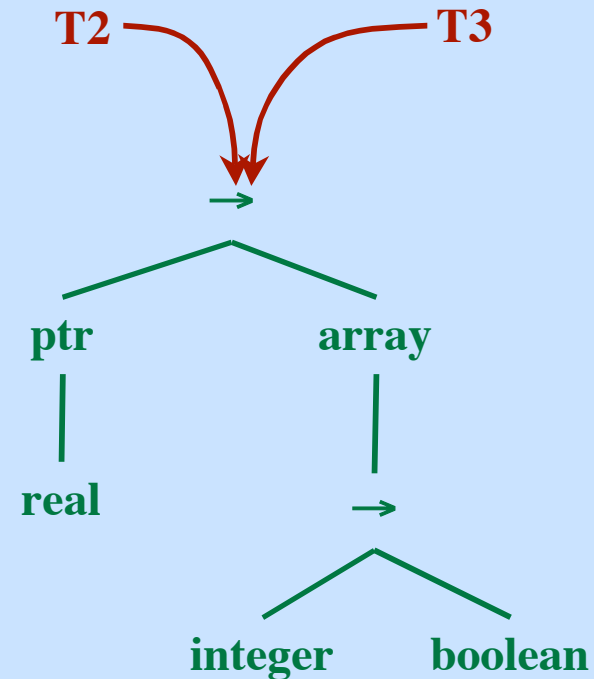
Must walk the trees to check.



### “Name Equivalence”

Are they the same tree?

Compare pointers



## Semantics - Part 1

### Testing Structural Equivalence

function typeEquiv (s, t) returns boolean

if (s and t are the same "basic" type) then  
return true

elseif (s = "array of s1") and (t = "array of t1") then  
return typeEquiv (s1, t1)

elseif (s = "s1 x s2") and (t = "t1 x t2") then  
return typeEquiv (s1, t1) and typeEquiv (s2, t2)

elseif (s = "ptr to s1") and (t = "ptr to t1") then  
return typeEquiv (s1, t1)

elseif (s = "s1 → s2") and (t = "t1 → t2") then  
return typeEquiv (s1, t1) and typeEquiv (s2, t2)

else  
return false

endIf

endFunction