Building LR Tables

How to construct the ACTION and GOTO tables?

- Define "items"
- Define "viable prefix"
- Define the "closure function"

Set-of-items → Set-of-items

- Define the GOTO function
- Work with a set of sets of items

A collection of sets of items

CC = Cannonical Collection of LR items

- Describe how to construct CC
- Given all this, describe how to construct the tables

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1

Syntax Analysis - Part 3

LR(0) Items

Given: A grammar, G

Items look like productions

... augmented with a dot in the righthand side.

Grammar:

1. $E \rightarrow E + T$ 2. $E \rightarrow T$ 3. $T \rightarrow T * F$ 4. $T \rightarrow F$ 5. $F \rightarrow (E)$ 6. $F \rightarrow \underline{id}$

The Items:

```
E \rightarrow \cdot E + T \qquad T \rightarrow \cdot F
E \rightarrow E \cdot + T \qquad T \rightarrow F \cdot
E \rightarrow E + \cdot T \qquad F \rightarrow \cdot (E)
E \rightarrow E + T \qquad F \rightarrow (\cdot E)
E \rightarrow \cdot T \qquad F \rightarrow (E \cdot)
E \rightarrow T \cdot \qquad F \rightarrow (E) \cdot
T \rightarrow \cdot T \star F \qquad F \rightarrow \cdot \underline{id}
T \rightarrow T \star \cdot F \qquad F \rightarrow \underline{id} \cdot
T \rightarrow T \star \cdot F \qquad F \rightarrow \underline{id} \cdot
```

Special Case:

Rule:

A -

Yields one item:

A → •

LR(1) Items

The look-ahead symbol

Just like before, except...

- Look-ahead symbol
- Terminal symbol from grammar

Grammar:

```
1. E \rightarrow E + T

2. E \rightarrow T

3. T \rightarrow T * F

4. T \rightarrow F

5. F \rightarrow (E)

6. F \rightarrow \underline{id}
```

Examples:

```
E \rightarrow \bullet E + T ,  
E \rightarrow \bullet E + T ,  
E \rightarrow E \bullet + T ,  
E \rightarrow E \bullet + T ,  
...
```

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-

1. $E \rightarrow E + T$ 2. $E \rightarrow T$

3. $T \rightarrow T * F$

5. $\mathbf{F} \rightarrow (\mathbf{E})$

 $T \rightarrow F$

6. $\mathbf{F} \rightarrow \mathbf{id}$

Syntax Analysis - Part 3

Intuition behind LR(1) Items

```
\mathbf{F} \rightarrow (\bullet \mathbf{E}),
```

We were hoping / expecting to see an ${\bf F}$ next, followed by a) and we have already seen a (.

We are on the path to finding an **F**, followed by a **)**.

Using rule 5, one way to find an \mathbf{F} is to find (\mathbf{E}) next.

So now we are looking for \mathbf{E}), followed by a).

```
\mathbf{F} \rightarrow (\mathbf{E}) \cdot , )
```

We were looking for an **F**, followed by a)

and we have found (\mathbf{E})

If a) comes next then the parse is going great!

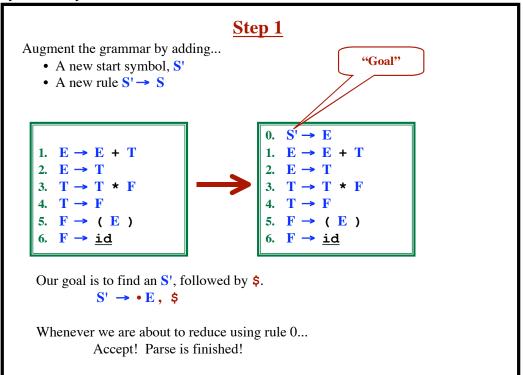
... Now reduce, using rule $\mathbf{F} \rightarrow (\mathbf{E})$

$E \rightarrow E + T$ 2. $\mathbf{E} \rightarrow \mathbf{T}$ **Intuition behind LR(1) Items** $T \rightarrow T * F$ $\mathbf{F} \rightarrow \bullet (\mathbf{E}),$ It would be legal at this point in the parse $\mathbf{F} \rightarrow (\mathbf{E})$ to see an F, followed by a). 6. $\mathbf{F} \rightarrow \mathbf{id}$ Using rule 5, one way to find an \mathbf{F} is to find (\mathbf{E}) next. So, among other possibilities, we are looking for (E), followed by a). If a (comes next, then let's scan it and keep going, looking for \mathbf{E}), followed by a). If we get \mathbf{E}) later, then we will be able to reduce it to \mathbf{F} ... but we may get something different (although perfectly legal). $\mathbf{E} \rightarrow \mathbf{T}$, It would be legal at this point in the parse to see an \mathbf{E} , followed by a). Using rule 2, one way to find an **E** is to find **T** next. So, among other possibilities, we are looking for a T followed by a). And how can we find a **T** followed by a)? $T \rightarrow \bullet T \star F$, $T \rightarrow \cdot F$,

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4

Syntax Analysis - Part 3



```
1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                              The CLOSURE Function
                                                                                        2. \mathbf{E} \rightarrow \mathbf{T}
Let's say we have this item:
                                                                                       3. T \rightarrow T * F
    E \rightarrow T,
                                                                                        4. T \rightarrow F
What are the ways to find a T?
                                                                                        5. \mathbf{F} \rightarrow (\mathbf{E})
    T \rightarrow F
    T \rightarrow T * F
We are looking for a T, followed by a ), so we'll need to add these items:
    T \rightarrow F,
    T \rightarrow T * F,
We can find a T followed by a ) if we find an F following by a ).
How can we find that?
    \mathbf{F} \rightarrow \bullet (\mathbf{E}),
    \mathbf{F} \rightarrow \bullet \underline{id},)
We can also find a T followed by a ) if we find an T * F following by a ).
To find that, we need to first find another T, but followed by \star.
    T \rightarrow F, \star
    T \rightarrow T * F, *
So we should also look for a F followed by a *.
    \mathbf{F} \rightarrow \bullet (\mathbf{E}), \star
    F → • id, *
```

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Syntax Analysis - Part 3

```
The CLOSURE Function
Given:
   I = a set of items
Output:
   CLOSURE(I) = a new set of items
Algorithm:
   result = {}
   add all items in I to result
   repeat
     for every item A \rightarrow \beta \cdot C \delta, a in result do
        for each rule C \rightarrow \gamma in the grammar do
           for each b in FIRST (\delta a) do
             add \mathbb{C} \rightarrow \gamma, \mathbf{b} to result
           endFor
        endFor
     endFor
   until we can't add anything more to result
```


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,

```
Syntax Analysis - Part 3
                                                                                                            0. S' \rightarrow E
                                                                                                            1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                   CLOSURE Function Example
                                                                                                            2. \mathbf{E} \rightarrow \mathbf{T}
                                                                                                            3. T \rightarrow T * F
     <u>Example:</u> Let I_1 = \{ E \rightarrow E \cdot + T, \}
                                                                                                            4. T \rightarrow F
                                            T \rightarrow T \cdot * F,
                                                                                                            5. \mathbf{F} \rightarrow (\mathbf{E})
                                            F \rightarrow id \cdot, )
                                                                                                            6. \mathbf{F} \rightarrow \mathbf{id}
                                            \mathbf{F} \rightarrow (\mathbf{E}) \cdot , )
     Compute: CLOSURE (I_1) = \{
           Start by adding all items in I...
                                                              E \rightarrow E \cdot + T,
                                                              T \rightarrow T \cdot * F,
                                                              \mathbf{F} \rightarrow \underline{id} \cdot , )
                                                              \mathbf{F} \rightarrow (\mathbf{E}) \cdot , )
```

$0. S' \rightarrow E$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$ **CLOSURE Function Example** 2. $\mathbf{E} \rightarrow \mathbf{T}$ <u>Example:</u> Let $I_1 = \{ E \rightarrow E \cdot + T, \}$ 3. $T \rightarrow T * F$ $T \rightarrow T \cdot \star F$, 5. $\mathbf{F} \rightarrow (\mathbf{E})$ $\mathbf{F} \rightarrow \underline{id} \cdot ,)$ 6. $\mathbf{F} \rightarrow \underline{id}$ $\mathbf{F} \rightarrow (\mathbf{E}) \cdot ,)$ **Compute:** CLOSURE $(I_1) = \{$ Start by adding all items in I... $E \rightarrow E \cdot + T$, $T \rightarrow T \cdot * F$, $\mathbf{F} \rightarrow \mathrm{id} \cdot ,)$ $\mathbf{F} \rightarrow (\mathbf{E}) \cdot ,)$ Is the dot in front of a non-terminal?

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11

```
Syntax Analysis - Part 3
```

```
0. S' \rightarrow E
                                                                                                     1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                             CLOSURE Function Example
                                                                                                     2. \mathbf{E} \rightarrow \mathbf{T}
                                                                                                     3. T \rightarrow T * F
<u>Example:</u> Let I_1 = \{ E \rightarrow E \cdot + T, \}
                                                                                                     4. T \rightarrow F
                                      T \rightarrow T \cdot * F,
                                                                                                     5. \mathbf{F} \rightarrow (\mathbf{E})
                                      \mathbf{F} \rightarrow \mathrm{id} \cdot,
                                                                                                     6. \mathbf{F} \rightarrow \mathbf{id}
                                      \mathbf{F} \rightarrow (\mathbf{E}) \cdot ,
Compute: CLOSURE (I_1) = \{
     Start by adding all items in I...
                                                       E \rightarrow E \cdot + T,
                                                       T \rightarrow T \cdot * F,
                                                       \mathbf{F} \rightarrow \underline{id} \cdot , )
                                                       \mathbf{F} \rightarrow (\mathbf{E}) \cdot , )
     Is the dot in front of a non-terminal?
     No... no more items are added.
                                                   }
```

CLOSURE Function Example

```
Example: Let I_2 = \{ T \rightarrow \bullet F, \}

T \rightarrow \bullet T \star F, \}

Compute: CLOSURE (I_2) = \{

Start by adding...
```

```
0. S' \rightarrow E

1. E \rightarrow E + T

2. E \rightarrow T

3. T \rightarrow T * F

4. T \rightarrow F

5. F \rightarrow (E)

6. F \rightarrow \underline{id}
```

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12

Syntax Analysis - Part 3

CLOSURE Function Example

```
Example: Let I_2 = \{ T \rightarrow \bullet F, \}
T \rightarrow \bullet T \star F, \}
Compute: CLOSURE (I_2) = \{ \}
Start by adding all items in I...
(1) T \rightarrow \bullet F, \}
(2) T \rightarrow \bullet T \star F, \}
```

Look at (1) first...

0. $S' \rightarrow E$ 1. $E \rightarrow E + T$ 2. $E \rightarrow T$ 3. $T \rightarrow T * F$ 4. $T \rightarrow F$ 5. $F \rightarrow (E)$ 6. $F \rightarrow \underline{id}$

Syntax Analysis - Part 3 $0. \quad \mathbf{S'} \rightarrow \mathbf{E}$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$ **CLOSURE Function Example** 2. $\mathbf{E} \rightarrow \mathbf{T}$ Example: Let $I_2 = \{ T \rightarrow F, \}$ 3. $T \rightarrow T * F$ $T \rightarrow T \star F,)$ CLOSURE $(I_2) = \{$ Compute: 5. $\mathbf{F} \rightarrow (\mathbf{E})$ Start by adding all items in I... F → <u>id</u> (1) $\mathbf{T} \rightarrow \mathbf{F}$, (2) $\mathbf{T} \rightarrow \mathbf{T} \star \mathbf{F}$, Look at (1) first. Look at each **F** rule. For every **b** in FIRST (ε) = $\{$) $\}$...

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15

```
Syntax Analysis - Part 3
                                                                                                                   0. S' \rightarrow E
                                                                                                                   1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                     CLOSURE Function Example
                                                                                                                   2. \mathbf{E} \rightarrow \mathbf{T}
                          Let I_2 = \{ T \rightarrow F, \}
      Example:
                                                                                                                  3. T \rightarrow T * F
                                           T \rightarrow \bullet T * F, ) }
                                                                                                                   4. T \rightarrow F
                          CLOSURE (I_2) = \{
      Compute:
                                                                                                                   5. \mathbf{F} \rightarrow (\mathbf{E})
            Start by adding all items in I...
                                                                                                                       \mathbf{F} \rightarrow \mathrm{id}
                                                            (1) \mathbf{T} \rightarrow \mathbf{F},
                                                            (2) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \ )
            Look at (1) first. Look at each F rule. For every b in FIRST (\varepsilon) = \{\}...
                                                           (3) \mathbf{F} \rightarrow \bullet (\mathbf{E}), )
                                                           (4) \mathbf{F} \rightarrow \bullet \underline{id},
            Look at (2) next...
```

CLOSURE Function Example

```
Example:
                  Let I_2 = \{ T \rightarrow F, \}
                                 T \rightarrow \bullet T * F, ) }
```

CLOSURE $(I_2) = \{$ Compute:

Start by adding all items in I...

(1) $\mathbf{T} \rightarrow \mathbf{F}$, $(2) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \)$

Look at (1) first. Look at each **F** rule. For every **b** in FIRST (ε) = $\{$) $\}$...

 $(3) \quad \mathbf{F} \rightarrow \bullet \quad (\mathbf{E}), \quad)$ $(4) \quad \mathbf{F} \rightarrow \bullet \mathbf{id},)$

Look at (2) next. Look at each **T** rule. For every **b** in FIRST (\star **F**) = { \star }...

(5) $\mathbf{T} \rightarrow \mathbf{F}, \star$

(6) $T \rightarrow T * F$, *

Look at (3) and (4) next...

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 $0. S' \rightarrow E$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$

3. $T \rightarrow T * F$

5. $\mathbf{F} \rightarrow (\mathbf{E})$

 $\mathbf{F} \rightarrow \mathbf{id}$

 $T \rightarrow F$

 $0. S' \rightarrow E$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$

2. $\mathbf{E} \rightarrow \mathbf{T}$

3. $T \rightarrow T \star F$

5. $\mathbf{F} \rightarrow (\mathbf{E})$

 $\mathbf{F} \rightarrow \mathrm{id}$

Syntax Analysis - Part 3

CLOSURE Function Example

```
Let I_2 = \{ T \rightarrow F, \}
Example:
                                 T \rightarrow \bullet T * F, ) }
```

CLOSURE $(I_2) = \{$ Compute:

Start by adding all items in I...

(1) $\mathbf{T} \rightarrow \mathbf{F}$, $(2) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \)$

Look at (1) first. Look at each \mathbf{F} rule. For every \mathbf{b} in FIRST ($\mathbf{\epsilon}$) = {)}...

(3) $\mathbf{F} \rightarrow \bullet (\mathbf{E}),)$ $(4) \quad \mathbf{F} \rightarrow \bullet \mathbf{id},)$

Look at (2) next. Look at each T rule. For every **b** in FIRST (*F) = $\{*\}$...

(5) $\mathbf{T} \rightarrow \mathbf{F}, \star$ (6) $T \rightarrow T * F, *$

Look at (3) and (4) next. The dot is not in front of a non-terminal.

Look at (5) next...

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Example:

CLOSURE Function Example Let $I_2 = \{ T \rightarrow \bullet F, \}$ $T \rightarrow \bullet T \star F, \}$ CLOSURE $(I_2) = \{ T \rightarrow \bullet F, \}$ $T \rightarrow \bullet T \star F, \}$ $T \rightarrow \bullet F, \}$ $T \rightarrow \bullet F, \}$ $T \rightarrow \bullet F, \}$

<u>Compute:</u> CLOSURE (I_2) = {
Start by adding all items in I...

 $(1) \quad \mathbf{T} \rightarrow \bullet \mathbf{F}, \)$ $(2) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \)$

Look at (1) first. Look at each F rule. For every **b** in FIRST (ε) = {)}...

(3) $\mathbf{F} \rightarrow \cdot (\mathbf{E})$,) (4) $\mathbf{F} \rightarrow \cdot \mathbf{id}$,

Look at (2) next. Look at each \mathbf{T} rule. For every \mathbf{b} in FIRST ($\mathbf{*F}$) = { $\mathbf{*}$ }...

(5) $\mathbf{T} \rightarrow \mathbf{F}, \star$ (6) $\mathbf{T} \rightarrow \mathbf{T} \star \mathbf{F}, \star$

Look at (3) and (4) next. The dot is not in front of a non-terminal.

Look at (5) next. Look at each **F** rule. For every **b** in FIRST ($\varepsilon \star$) = { \star }...

(7) $\mathbf{F} \rightarrow \bullet (\mathbf{E}), \star$ (8) $\mathbf{F} \rightarrow \bullet \underline{id}, \star$

Look at (6) next...

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10

0. S' → E
1. E → E + T

3. $T \rightarrow T * F$

5. $\mathbf{F} \rightarrow (\mathbf{E})$

 $\mathbf{F} \rightarrow \mathrm{id}$

 $T \rightarrow F$

 $0. S' \rightarrow E$

 $\mathbf{F} \rightarrow \mathrm{id}$

```
Syntax Analysis - Part 3
```

```
CLOSURE Function Example
```

```
Example: Let I_2 = \{ T \rightarrow \bullet F, \}

T \rightarrow \bullet T \star F, \}
```

 $\underline{Compute:}$ CLOSURE (I_2) = {

Start by adding all items in I...

(1) $T \rightarrow F$,) (2) $T \rightarrow T \times F$,)

Look at (1) first. Look at each \mathbf{F} rule. For every \mathbf{b} in FIRST ($\mathbf{\epsilon}$) = {)}...

(3) $\mathbf{F} \rightarrow \cdot (\mathbf{E})$,) (4) $\mathbf{F} \rightarrow \cdot \mathbf{id}$,

Look at (2) next. Look at each \mathbf{T} rule. For every \mathbf{b} in FIRST (* \mathbf{F}) = {*}...

(5) $\mathbf{T} \rightarrow \bullet \mathbf{F}, \star$ (6) $\mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \star$

Look at (3) and (4) next. The dot is not in front of a non-terminal.

Look at (5) next. Look at each **F** rule. For every **b** in FIRST ($\varepsilon \star$) = { \star }...

 $(7) \quad \mathbf{F} \rightarrow \bullet \quad (\mathbf{E}), \quad \star$

(8) $\mathbf{F} \rightarrow \bullet \underline{id}, \star$

Look at (6) next. Look at each **T** rule. For every **b** in FIRST (***F***) = {*}...

We already added (5) and (6)

Look at (7) and (8) next...

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$0. S' \rightarrow E$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$ **CLOSURE Function Example** 2. $\mathbf{E} \rightarrow \mathbf{T}$ Example: Let $I_2 = \{ T \rightarrow F, \}$ $T \rightarrow T * F$ $T \rightarrow \bullet T * F,) }$ Compute: CLOSURE $(I_2) = \{$ 5. $\mathbf{F} \rightarrow (\mathbf{E})$ Start by adding all items in I... $\mathbf{F} \rightarrow \mathrm{id}$ (1) $\mathbf{T} \rightarrow \mathbf{F}$, $(2) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \)$ Look at (1) first. Look at each F rule. For every **b** in FIRST (ε) = {)}... $(3) \quad \mathbf{F} \rightarrow \bullet \quad (\mathbf{E}), \quad)$ $(4) \quad \mathbf{F} \rightarrow \bullet \mathbf{id},)$ Look at (2) next. Look at each T rule. For every **b** in FIRST ($\star F$) = { \star }... (5) $\mathbf{T} \rightarrow \mathbf{F}, \star$ $(6) \quad \mathbf{T} \rightarrow \bullet \mathbf{T} \star \mathbf{F}, \ \star$ Look at (3) and (4) next. The dot is not in front of a non-terminal. Look at (5) next. Look at each **F** rule. For every **b** in FIRST ($\varepsilon \star$) = { \star }... (7) $\mathbf{F} \rightarrow \bullet (\mathbf{E}), \star$ (8) $\mathbf{F} \rightarrow \bullet \underline{id}, \star$ Look at (6) next. Look at each T rule. For every **b** in FIRST ($\star F \star$) = { \star }... We already added (5) and (6) Look at (7) and (8) next. The dot is not in front of a non-terminal. }

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2

```
Syntax Analysis - Part 3
                                                                                                            0. S' \rightarrow E
                                                                                                             1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                   CLOSURE Function Example
     Example:
                         Let I_3 = \{ \mathbf{E} \rightarrow \bullet \mathbf{E} + \mathbf{T}, \}
                                                                                                            3. T \rightarrow T * F
     Compute:
                         CLOSURE (I_3) = \{
                                                                                                                T \rightarrow F
                                                                                                            5. \mathbf{F} \rightarrow (\mathbf{E})
                                                        E \rightarrow E + T,
           Look at E rules. For every b in FIRST (+T) = \{+\}...
                                                                                                                 \mathbf{F} \rightarrow \mathrm{id}
                                                        \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}, +
                                                        E \rightarrow T, +
           Look at E rules. For every b in FIRST (+T+)... (Nothing new added)
           Look at T rules. For every b in FIRST (\varepsilon+) = {+}
                                                        T \rightarrow \bullet T \star F_{\bullet} +
                                                        T \rightarrow F, +
           Look at T rules. For every b in FIRST (\star F+) = {\star}
                                                        T \rightarrow T * F, *
                                                        T \rightarrow \bullet F, *
           Look at F rules. For every b in FIRST (\varepsilon+) = {+}
                                                        \mathbf{F} \rightarrow \bullet (\mathbf{E}), +
                                                        F \rightarrow \bullet id, +
           Look at F rules. For every b in FIRST (\varepsilon \star) = {\star}
                                                        \mathbf{F} \rightarrow \bullet (\mathbf{E}), \star
                                                        \mathbf{F} \rightarrow \bullet \underline{id}, *
                                                     }
```

The GOTO Function Let I be a set of items... Let X be a grammar symbol (terminal or non-terminal)... function GOTO(I,X) returns a set of items In other words, move result = {} the dot past the X look at all items in I... in any items where it if $A \rightarrow \alpha \cdot X \delta$, a is in I is in front of an X then add $A \rightarrow \alpha X \cdot \delta$, a to result result = CLOSURE (result) ...and take the CLOSURE of whatever items you get © Harry H. Porter, 2005

Syntax Analysis - Part 3

```
The GOTO Function
Let I be a set of items...
Let X be a grammar symbol (terminal or non-terminal)...
function GOTO(I,X) returns a set of items
                                                           In other words, move
   result = {}
                                                             the dot past the X
   look at all items in I...
                                                           in any items where it
      if A \rightarrow \alpha \cdot X \delta, a is in I
                                                             is in front of an X
         then add A \rightarrow \alpha X \cdot \delta, a to result
   result = CLOSURE (result).
                                                     ...and take the CLOSURE
                                                     of whatever items you get
Intuition:
   • I is a set of items indicating where we are so far,
         after seeing some prefix y of the input.
   • I describes what we might legally see next.
   • Assume we get an X next.
   • Now we have seen some prefix \gamma X of the input.
   • GOTO(I, X) tells what we could legally see after that.
   • GOTO(I, X) is the set of all items that are "valid" for prefix \gamma X.
```

GOTO Function Example 2. $\mathbf{E} \rightarrow \mathbf{T}$ **Example:** Let $I_4 = \{ E \rightarrow T \cdot, \}$ 3. $T \rightarrow T * F$ $T \rightarrow T \cdot \star F$,) } **Compute:** GOTO $(I_4, \star) = \{$ 5. $\mathbf{F} \rightarrow (\mathbf{E})$ Is the • in front of * in any of the items? $\mathbf{F} \rightarrow \underline{\mathbf{id}}$ $T \rightarrow T * \cdot F$, Now take the closure... $\mathbf{F} \rightarrow \bullet (\mathbf{E}),$ Intuition: We found a T and then we found a *. What are we looking for next? $T \rightarrow T * \cdot F$, Means: We are now looking for an F followed by) $\mathbf{F} \rightarrow \bullet (\mathbf{E}),$ Means: We could find that by finding (E) followed by) $F \rightarrow \bullet id$,) Means: We could find that by finding (E) followed by)

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```
Syntax Analysis - Part 3
```

```
0. S' \rightarrow E
                                                                                     1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                            GOTO Function Example
<u>Example:</u> Let I_5 = \{ E \rightarrow \bullet T, \}
                                                                                     3. T \rightarrow T * F
                               T \rightarrow T * F, ) }
Compute: GOTO (I_5, T) = \{
                                                                                     5. \mathbf{F} \rightarrow (\mathbf{E})
    Is the • in front of T in any of the items?
                                                                                        \mathbf{F} \rightarrow \mathrm{id}
                                        E \rightarrow T \cdot , )
                                        T \rightarrow T \cdot * F,
    Now take the closure...
               Is the • in from of any non-terminal? Nothing more added...
                                       }
Intuition:
  We were looking for a T. Then we found it. What are we looking for next?
     E \rightarrow T \cdot , )
               Means: We are now looking for )
     T \rightarrow T \cdot *F,
               Means: We are now looking for * F followed by )
```

Each CC_i will be a set of items.

Constructing the Canonical Collection

```
We will build up a collection of these.

\mathbb{CC} = "The Canonical Collection of LR(1) items"

= a set of sets of items
```

```
= a set of sets of items
= \{ CC_0, CC_1, CC_2, CC_3, \dots CC_N \}
```

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2

Syntax Analysis - Part 3

Constructing the Canonical Collection

```
Each CC<sub>i</sub> will be a set of items.
```

We will build up a collection of these.

```
\mathbb{CC} = \text{``The Canonical Collection of LR(1) items''}
= a \text{ set of sets of items}
= \{ CC_0, CC_1, CC_2, CC_3, \dots CC_N \}
```

Algorithm to construct \mathbb{CC} , the Canonical Collection of LR(1) Items:

```
\begin{array}{l} \text{Algorithm to Construct CC, the Canonical Collection of } Ek(f) \text{ Thems.} \\ \\ \text{let } CC_0 = \text{CLOSURE}\left(\left\{S' \to \bullet S, \right.\right\}\right) \\ \text{add } CC_0 \text{ to } \mathbb{CC} \\ \\ \underline{\text{repeat}} \\ \\ \text{let } CC_i \text{ be some set of items already in } \mathbb{CC} \\ \underline{\text{for each }} X \text{ (that follows a } \bullet \text{ in some item in } CC_i) \dots \\ \\ \text{compute } CC_k = \text{GOTO}\left(CC_i, X\right) \\ \underline{\text{if }} CC_k \text{ is not already in } \mathbb{CC} \\ \underline{\text{then}} \\ \text{add it} \\ \text{set MOVE}(CC_i, X) = CC_k \\ \underline{\text{endIf}} \\ \underline{\text{endFor}} \\ \underline{\text{until}} \text{ nothing more can be added to } \mathbb{CC} \\ \end{array}
```

```
Syntax Analysis - Part 3
                                                                                                                                                0. \quad \mathbf{S'} \rightarrow \mathbf{E}
                                                                                                                                                1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                                                            Example:
                                                                                                                                                2. \mathbf{E} \rightarrow \mathbf{T}
       CC_0 = CLOSURE(\{S' \rightarrow \bullet E, \$\})
                                                                                                                                                3. T \rightarrow T * F
                  = \{ S' \rightarrow E, $
                                                                                                                                                4. T \rightarrow F
                           \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}, $
                                                                                                                                                5. \mathbf{F} \rightarrow (\mathbf{E})
                           \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}, +
                                                                                                                                                6. \mathbf{F} \rightarrow \underline{id}
                           \mathbf{E} \rightarrow \mathbf{T}, $
                           E \rightarrow T, +
                           T \rightarrow \bullet T \star F, $
                           T \rightarrow \bullet T * F . +
                           T \rightarrow \bullet T \star F, \star
                           T \rightarrow \cdot F, $
                           T \rightarrow \bullet F, +
                           T \rightarrow \bullet F, *
                           \mathbf{F} \rightarrow \bullet (\mathbf{E}), $
                           \mathbf{F} \rightarrow \bullet (\mathbf{E}), +
                           \mathbf{F} \rightarrow \bullet (\mathbf{E}), \star
                           F \rightarrow \bullet id, $
                           \mathbf{F} \rightarrow \bullet \mathrm{id}, +
                           \mathbf{F} \rightarrow \bullet \underline{id}, \star \}
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```

```
Syntax Analysis - Part 3
                                                                                                                                          0. S' \rightarrow E
                                                                                                                                          1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                                                         Example:
                                                                                                                                          2. \mathbf{E} \rightarrow \mathbf{T}
       CC_0 = CLOSURE(\{S' \rightarrow \bullet E, \$\})
                                                                                                                                         3. T \rightarrow T * F
                 = \{ S' \rightarrow E, \$
                                                                                                                                          4. T \rightarrow F
                          \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}, $
                                                                                                                                          5. \mathbf{F} \rightarrow (\mathbf{E})
                          \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}, +
                                                                                                                                          6. \mathbf{F} \rightarrow \mathbf{id}
                          \mathbf{E} \rightarrow \mathbf{T}, $
                          E \rightarrow T, +
                          T \rightarrow \bullet T \star F, $
                          T \rightarrow \bullet T \star F, +
                          T \rightarrow \bullet T * F , *
                                                                                    The • is before \mathbf{E}, \mathbf{T}, \mathbf{F}, \mathbf{id}, and \mathbf{C}...
                          T \rightarrow \bullet F, $
                          T \rightarrow \cdot F, +
                                                                                    Next, we'll compute...
                          T \rightarrow \bullet F, *
                                                                                                       GOTO(CC_0, \mathbf{E})
                                                                                                                                             \Rightarrow CC<sub>1</sub>
                          \mathbf{F} \rightarrow \bullet (\mathbf{E}), \$
                                                                                                                                             \Rightarrow CC<sub>2</sub>
                                                                                                       GOTO(CC_0, T)
                          \mathbf{F} \rightarrow \bullet (\mathbf{E}), +
                                                                                                       GOTO(CC_0, \mathbf{F})
                                                                                                                                             \Rightarrow CC<sub>3</sub>
                          \mathbf{F} \rightarrow \bullet (\mathbf{E}), \star
                                                                                                       GOTO(CC_0, \underline{id}) \Rightarrow CC_5
                          F \rightarrow \bullet id, $
                                                                                                                                             \Rightarrow CC<sub>4</sub>
                                                                                                       GOTO(CC_0, ()
                          \mathbf{F} \rightarrow \bullet \mathrm{id}, +
                          \mathbf{F} \rightarrow \bullet \mathsf{id}, \star
```

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$\underline{GOTO}(\underline{CC_0}, \underline{E}) = \underline{CC_1}$

```
Advance • past \mathbf{E} in the items containing • \mathbf{E} CC_1 = \{
```

 $S' \rightarrow E \cdot , \$$ $E \rightarrow E \cdot + T , \$$ $E \rightarrow E \cdot + T , +$

And take the closure... (Nothing more added.)

Intuition:

We will reduce by $S' \rightarrow E$ if the next symbol is \$. Otherwise, we we will look for a + next.

The • is in front of +. We'll come back to CC₁ later.

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31

 $0. \quad \mathbf{S'} \rightarrow \mathbf{E}$

1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$

Syntax Analysis - Part 3

$\underline{\mathbf{GOTO}\;(\mathbf{CC}_{\underline{0}},\mathbf{T})=\mathbf{CC}_{\underline{2}}}$

```
Advance • past T
CC_2 = \{ E \rightarrow T \cdot , \$ 
E \rightarrow T \cdot , + 
T \rightarrow T \cdot *F , \$ 
T \rightarrow T \cdot *F , + 
T \rightarrow T \cdot *F , *
```

And take the closure...

}

Intuition:

We will reduce by $T \rightarrow F$ if the next symbol is \$ or +. Otherwise, we will look for *.

The • is in front of *. We'll come back to CC₂ later.

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GOTO $(CC_0, F) = CC_3$ 1. $E \rightarrow E$ 2. $E \rightarrow T$ 3. $T \rightarrow T$

```
Advance • past \mathbf{F}
CC_3 = \{ \\ \mathbf{T} \rightarrow \mathbf{F} \bullet, \$ \\ \mathbf{T} \rightarrow \mathbf{F} \bullet, + \\ \mathbf{T} \rightarrow \mathbf{F} \bullet, *
```

And take the closure...

}

Intuition:

We will reduce by $T \rightarrow F$ if the next symbol is \$, +, or *.

The • is not in front of any symbol; no further "GOTO"s.

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31

Syntax Analysis - Part 3

$\underline{\mathbf{GOTO}\;(\mathbf{CC}_{\underline{0}},\mathtt{id}\;)=\mathbf{CC}_{\underline{5}}}$

```
Advance • past \underline{id}
CC_5 = \{ F \rightarrow \underline{id} \cdot, \$ 
F \rightarrow \underline{id} \cdot, +
```

And take the closure...

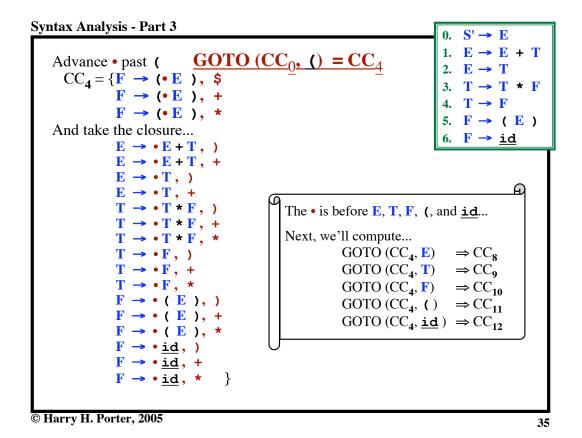
}

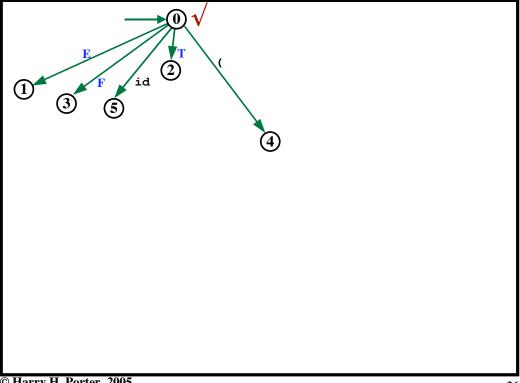
Intuition:

We will reduce after seeing an <u>id</u>, if the next symbol is +, *, or \$.

The • is not in front of any symbol; no further "GOTO"s.

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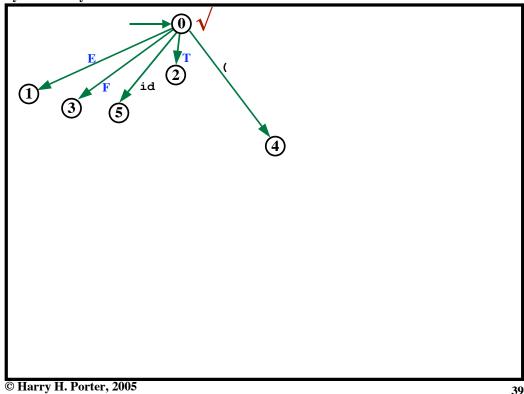
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Syntax Analysis - Part 3 $0. S' \rightarrow E$ 1. $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$ $\underline{\mathbf{GOTO}(\mathbf{CC}_1,+)} = \underline{\mathbf{CC}_6}$ 2. $\mathbf{E} \rightarrow \mathbf{T}$ 3. $T \rightarrow T * F$ $E \rightarrow E \cdot + T$, \$ 4. $T \rightarrow F$ $\mathbf{E} \rightarrow \mathbf{E} \cdot + \mathbf{T}$, + 5. $\mathbf{F} \rightarrow (\mathbf{E})$ Advance • past + in the items containing • + 6. $\mathbf{F} \rightarrow \mathbf{id}$ $CC_6 = \{ E \rightarrow E + \bullet T, \$$ $E \rightarrow E + \cdot T$, + And take the closure... $T \rightarrow T * F$, \$ $T \rightarrow T * F +$ $T \rightarrow T * F, *$ $T \rightarrow \bullet F$, \$ $T \rightarrow F$, + $T \rightarrow \bullet F$, * $\mathbf{F} \rightarrow \bullet (\mathbf{E}), \$$ $\mathbf{F} \rightarrow \bullet (\mathbf{E}), +$ $\mathbf{F} \rightarrow \bullet (\mathbf{E}), \star$ $\mathbf{F} \rightarrow \bullet \text{id}, \$$ $F \rightarrow \bullet id, +$ $F \rightarrow \bullet id, *$ }

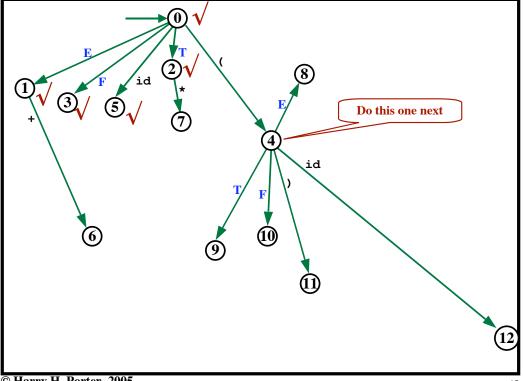
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3

```
Syntax Analysis - Part 3
                                                                                                                                                  0. S' \rightarrow E
                                                                                                                                                  1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                                          \underline{\mathbf{GOTO}\;(\mathbf{CC}_{\underline{2}},\,\star)=\mathbf{CC}_{\underline{7}}}
                                                                                                                                                 2. \mathbf{E} \rightarrow \mathbf{T}
       CC_2 = \{
                                                                                                                                                 3. T \rightarrow T * F
                              E \rightarrow T \cdot , $
                                                                                                                                                  4. T \rightarrow F
                              E \rightarrow T \cdot , +
                              T \rightarrow T \cdot \star F, $
                                                                                                                                                  5. \mathbf{F} \rightarrow (\mathbf{E})
                             T \rightarrow T \cdot \star F, +
T \rightarrow T \cdot \star F, \star
                                                                                                                                                  6. \mathbf{F} \rightarrow \mathrm{id}
       Advance • past *
          CC_7 = \{
                              T \rightarrow T * \cdot F, $
                              T \rightarrow T * \cdot F +
                             T \rightarrow T \star \bullet F, \star
       And take the closure...
                              \mathbf{F} \rightarrow \bullet (\mathbf{E}), $
                              \mathbf{F} \rightarrow \bullet (\mathbf{E}), +
                              \mathbf{F} \rightarrow \bullet (\mathbf{E}), \star
                              F → • <u>id</u>, $
                              \mathbf{F} \rightarrow \mathbf{\dot{\underline{id}}}, +
                              F \rightarrow \bullet id, *
       Intuition:
                   We have found T \star.
                   Next, look for a F followed by $, +, or *.
```



Syntax Analysis - Part 3



Syntax Analysis - Part 3 $\begin{array}{c} GOTO(CC_4, E) = CC_8 \\ CC_8 = \{ \\ F \rightarrow (E \cdot), \$ \\ F \rightarrow (E \cdot), * \\ E \rightarrow E \cdot + T,) \\ E \rightarrow E \cdot + T, + \\ And take the closure... \end{array}$ © Harry H. Porter, 2005

```
Syntax Analysis - Part 3

\frac{\text{GOTO (CC}_{4}, \text{T}) = \text{CC}_{9}}{\text{CC}_{9} = \{}

\frac{\text{E} \rightarrow \text{T} \cdot , \text{ }}{\text{E} \rightarrow \text{T} \cdot * \text{F}, \text{ }}

\frac{\text{T} \rightarrow \text{T} \cdot * \text{F}, \text{ }}{\text{T} \rightarrow \text{T} \cdot * \text{F}, \text{ }}

And take the closure...

\frac{\text{COTO (CC}_{4}, \text{T}) = \text{CC}_{9}}{\text{CC}_{9}}
```

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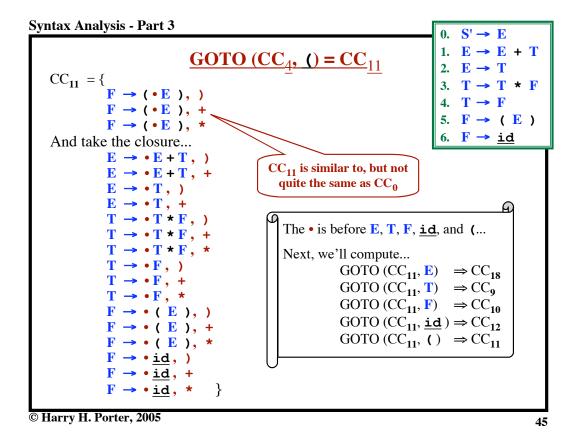
Syntax Analysis - Part 3 $GOTO (CC_4, F) = CC_{10}$ $CC_{10} = \{ T \rightarrow F \bullet, + \\ T \rightarrow F \bullet, *$ And take the closure... $}$ © Harry H. Porter, 2005 $0. S' \rightarrow E$ 1. $E \rightarrow E + T$ 2. $E \rightarrow T$ 3. $T \rightarrow T \star F$ 4. $T \rightarrow F$ 5. $F \rightarrow (E)$ 6. $F \rightarrow \underline{id}$

```
Syntax Analysis - Part 3

\begin{array}{c}
GOTO (CC_{4}, id) = CC_{12} \\
CC_{12} = \{ \\
F \rightarrow \underline{id} \cdot, \\
F \rightarrow \underline{id} \cdot, + \\
F \rightarrow \underline{id} \cdot, \star \\
And take the closure...
\end{array}

\begin{array}{c}
0. \quad S' \rightarrow E \\
1. \quad E \rightarrow E + T \\
2. \quad E \rightarrow T \\
3. \quad T \rightarrow T \star F \\
4. \quad T \rightarrow F \\
5. \quad F \rightarrow (E) \\
6. \quad F \rightarrow \underline{id}
\end{array}
```

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```
Syntax Analysis - Part 3
                                                                                                                                                  0. S' \rightarrow E
                                                       \underline{\mathbf{GOTO}\ (\mathbf{CC}_{\underline{11}}, \mathbf{E}) = \mathbf{CC}_{\underline{18}}}
                                                                                                                                                   1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                                                                                                                                  2. \mathbf{E} \rightarrow \mathbf{T}
                                                                                                                                                  3. T \rightarrow T * F
                            \mathbf{F} \rightarrow (\mathbf{E} \cdot), )
                                                                                                                                                  4. T \rightarrow F
                           \mathbf{F} \rightarrow (\mathbf{E} \cdot), +
                                                                                                                                                  5. \mathbf{F} \rightarrow (\mathbf{E})
                           \mathbf{F} \rightarrow (\mathbf{E} \bullet), \star
                                                                                                                                                   6. \mathbf{F} \rightarrow \mathrm{id}
                           E \rightarrow E \cdot + T,
                           E \rightarrow E \cdot + T, +
       And take the closure...
                        }
```

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Syntax Analysis - Part 3 $GOTO (CC_{11}, T) = CC_{9}$ $CC_{9} = \{ E \rightarrow T \cdot,) E \rightarrow T \cdot, + T \rightarrow T \cdot *F, + T \rightarrow T \cdot *F, *$ And take the closure... $}$ We have seen CC₉ before! $0. S' \rightarrow E 1. E \rightarrow E + T 2. E \rightarrow T 3. T \rightarrow T *F 4. T \rightarrow F 5. F \rightarrow (E) 6. F \rightarrow id$

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4

```
Syntax Analysis - Part 3

GOTO (CC_{11}, F) = CC_{10}

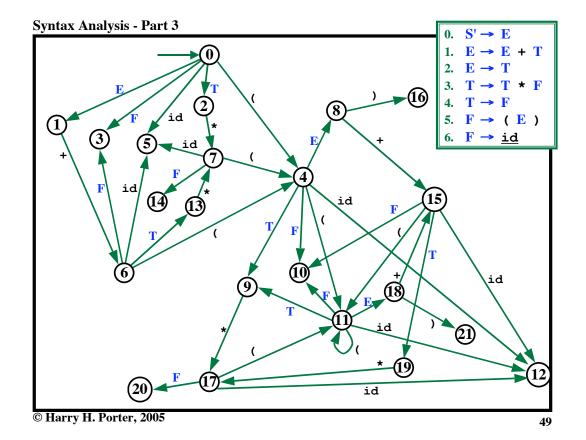
CC_{10} = \{
T \rightarrow F \circ, )
T \rightarrow F \circ, *
T \rightarrow F \circ, *

And take the closure...

}

We have seen CC_{10} before!

0. S' \rightarrow E
1. E \rightarrow E + T
2. E \rightarrow T
3. T \rightarrow T * F
4. T \rightarrow F
5. F \rightarrow (E)
6. F \rightarrow \underline{id}
```



Viable Prefixes

Consider a right-sentential form

$$S \Rightarrow_{RM}^* XXAfff \Rightarrow_{RM} XXBCDEfff \Rightarrow_{RM} ...$$

Rule: Handle

 $A \rightarrow BCDE$

A viable prefix is a prefix of a right sentential form that does not extend to the right end of the handle.

Viable Prefixes

Consider a right-sentential form

$$S \Rightarrow_{RM}^* XXAfff \Rightarrow_{RM} XXBCDEfff \Rightarrow_{RM} ...$$
Rule:

 $A \rightarrow BCDE$

A viable prefix is a prefix of a right sentential form that does not extend to the right end of the handle.

XXBCDEfff

A Viable prefix

Given a viable prefix, we can always add terminals to get a right-sentential form!

Why?

Assume that XXBC is a viable prefix that we've shifted onto the stack.

Assume that we have some more terminals **dddeeefff** in the input.

If this string is legal, there must be rules that allow

 $D\Rightarrow^* \mathbf{ddd}$ and $E\Rightarrow^* \mathbf{eee}$ $S ... \Rightarrow_{\mathbf{RM}}^* \underline{XXBCDE}\mathbf{fff} \Rightarrow_{\mathbf{RM}} \underline{XXBCD}\mathbf{eeefff} \Rightarrow_{\mathbf{RM}} \underline{XXBC}\mathbf{ddd}\mathbf{eeefff}$

As long as we have a viable prefix, just keep shifting!

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51

Syntax Analysis - Part 3

The Main Idea of LR Parsing

As long as what is on the stack is a viable prefix...

• The unseen terminals might be what is required to make STACK || REMAINING-INPUT

into a right-sentential form.

• We are on course to finding a rightmost derivation.

The key ideas of LR parsing:

Construct a DFA to recognize viable prefixes!

Every path in the DFA (from start to any final or non-final state) describes a viable prefix.

Each state is a set of items.

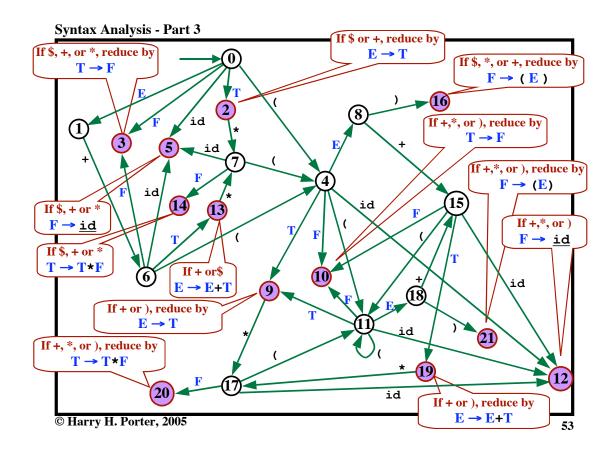
If the DFA has an edge from the current state labeled with a terminal And the edge label = the lookahead symbol

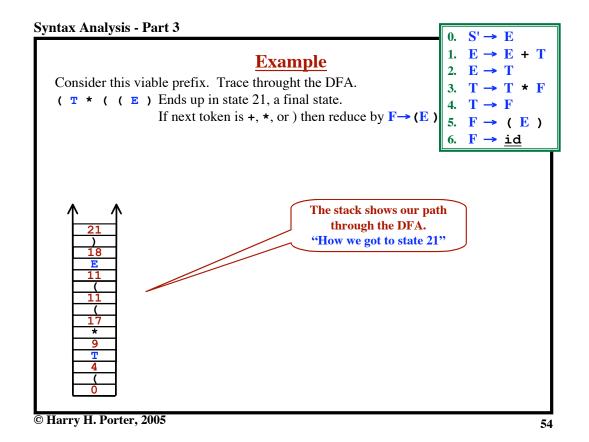
Do a shift: Add this terminal to the viable prefix.

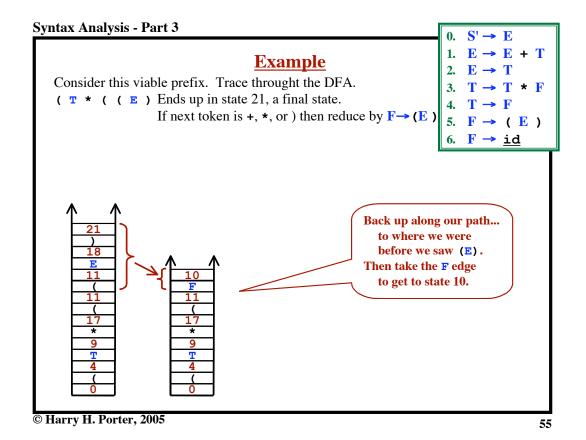
When the dot is at the end of one of the items in a state...

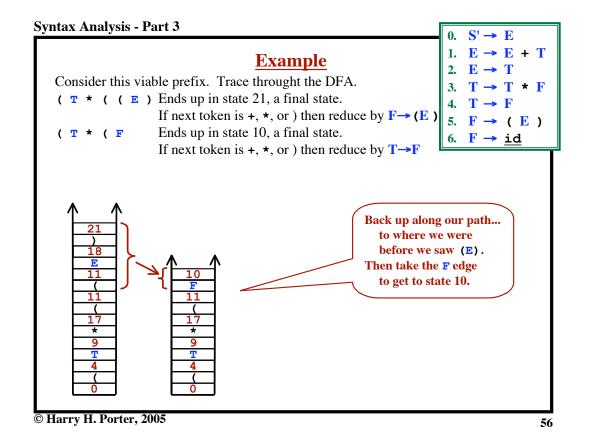
If the next symbol = the lookahead symbol...

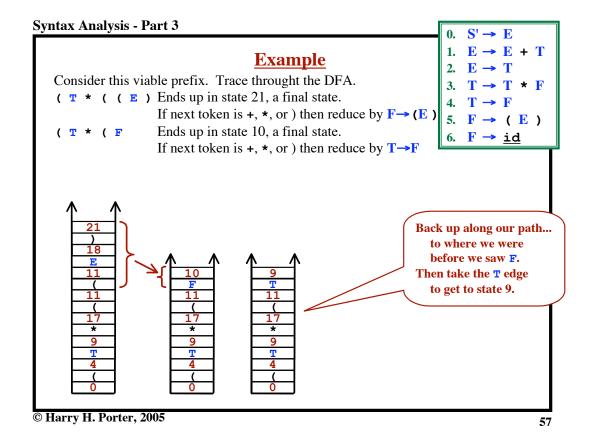
Do a reduction. A \rightarrow XYZ

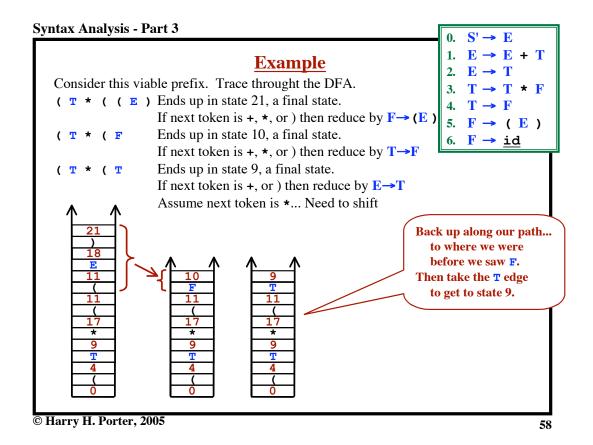


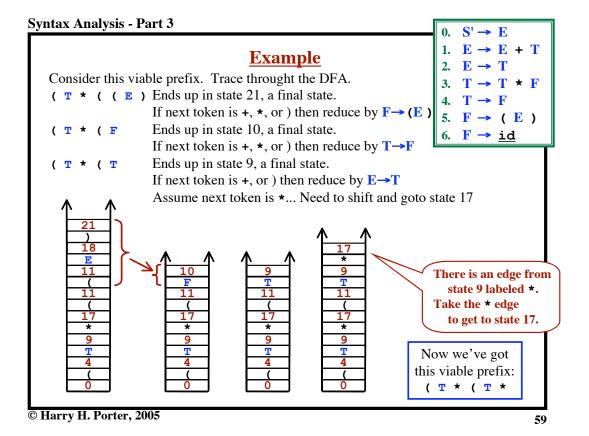












```
Syntax Analysis - Part 3
                                                                                         S' \rightarrow E
                                                                                     1. \mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}
                                       Other Examples
    Here are some viable prefixes.
                                                                                         T \rightarrow T * F
    Trace through the DFA for each of these!
                                                                                     5. \mathbf{F} \rightarrow (\mathbf{E})
         (E + T * F
                                                                                        \mathbf{F} \rightarrow \mathrm{id}
                Goes to state 20, a final state.
                If next token is \$, +, or * then reduce by T \rightarrow T * F
        E + ( ( ( T * id
                Goes to state 12, a final state.
                If next token is +, *, or ) then reduce by F \rightarrow \underline{id}
         (E+(E+(E+(E+(T*(T*(T*
                Goes to state 17, not a final state.
                We must get \mathbf{F}, (, or \underline{id} next
         (E + (T
                Goes to state 9
                If next token is ( or + then reduce by E \rightarrow T
                Else okay to see *
```

Algorithm to Construct ACTION and GOTO Tables Input: Grammar G, augmented with $S' \rightarrow S$ **Output:** ACTION and GOTO Tables Construct "Canonical Collection of LR(1) items" along with MOVE function. $\mathbb{CC} = \{ CC_0, CC_1, CC_2, CC_3, \dots CC_N \}$ There will be N states, one per set of items $\{0, 1, 2, 3, ... N\}$ for each CC_i do for each item in CC; do if the item has the form $A \rightarrow \beta \cdot c \gamma$, a and MOVE (CC_i , c) = CC_i then set ACTION[i,c] to "Shift j" elseIf the item has the form $A \rightarrow \beta \cdot ,a$ then set ACTION[i,a] to "Reduce $A \rightarrow \beta$ " elseIf the item has the form $S' \rightarrow S \cdot , $$ then set ACTION[i, \$] to "Accept" endFor for each nonterminal A do \underline{if} MOVE (CC_i, \underline{A}) = CC_i \underline{then} set GOTO[i, A] to j endIf endFor endFor

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61

Syntax Analysis - Part 3

The SLR Table Construction Algorithm

With SLR, we do not have the lookahead symbol.

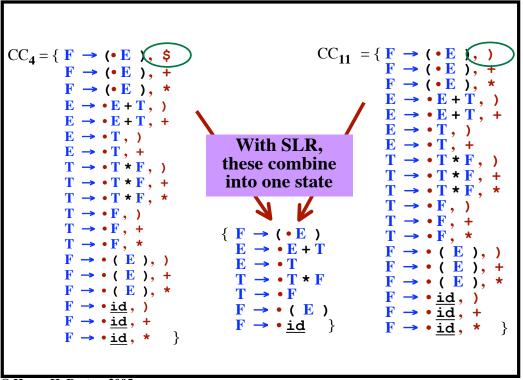
```
\begin{array}{cccc} \underline{LR(1) \text{ items:}} & \underline{LR(0) \text{ items:}} \\ F \rightarrow (\bullet E), & & & \\ F \rightarrow (\bullet E), & + & \\ F \rightarrow (\bullet E), & * & & \\ \end{array}
```

Some information is lost.

Some states in \mathbb{CC} collapse into one state.

There are fewer states in \mathbb{CC}

 \Rightarrow Fewer rows in the resulting tables.



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6

Syntax Analysis - Part 3

The SLR Table Construction Algorithm

The CLOSURE function is basically the same, but simpler.

The GOTO function is basically the same, but simpler.

The Construction of the Canonical Collection is the same.

The Construction of the ACTION and GOTO tables is a little different.

```
elseIf the item has the form A \to \beta • ,a then set ACTION[i,a] to "Reduce A \to \beta'' ...

...

elseIf the item has the form A \to \beta • then for all b in FOLLOW(A) do set ACTION[i,b] to "Reduce A \to \beta'' endFor ...
```

Sometimes SLR may try to put two actions in one table entry ...while the LR(1) tables would have more states, more rows, and no conflicts.

SLR: The CLOSURE Function Given: I = a set of LR(0) itemsOutput: CLOSURE(I) = a new set of items Algorithm: result = {} add all items in I to result repeat for every item $A \rightarrow \beta \cdot C \delta$ in result do for each rule $C \rightarrow \gamma$ in the grammar do add $\mathbb{C} \rightarrow \bullet \gamma$ to result endFor endFor until we can't add anything more to result © Harry H. Porter, 2005

Syntax Analysis - Part 3

```
SLR: The GOTO Function
Let I be a set of items...
Let X be a grammar symbol (terminal or non-terminal)...
function GOTO(I,X) returns a set of items
                                                        In other words, move
   result = {}
                                                          the dot past the X
   look at all items in I...
                                                         in any items where it
     if A \rightarrow \alpha \cdot X \delta is in I
                                                          is in front of an X
        then add A \rightarrow \alpha X \cdot \delta to result
   result = CLOSURE(result)
                                                   ...and take the CLOSURE
                                                   of whatever items you get
```

SLR: Constructing the Canonical Collection Each CC_i will be a set of items. We will build up a collection of these. \mathbb{CC} = "The Canonical Collection of LR(0) items" = a set of sets of items $= \{ \ \mathsf{CC}_0, \mathsf{CC}_1, \mathsf{CC}_2, \mathsf{CC}_3, \dots \mathsf{CC}_N \}$ Algorithm to construct \mathbb{CC} , the Canonical Collection of LR(1) Items: let $CC_0 = CLOSURE(\{S' \rightarrow \bullet S, \$\})$ $\operatorname{\mathbf{add}}\operatorname{CC}_0\operatorname{to}\operatorname{\mathbb{C}}\operatorname{\mathbb{C}}$ repeat let CC_i be some set of items already in \mathbb{CC} for each X (that follows a • in some item in CC_i)... compute $CC_k = GOTO(CC_i, X)$ $\underline{\text{if}} \; \mathrm{CC}_k \, \text{is not already in} \; \mathbb{CC} \, \underline{\text{then}}$ add it $set MOVE(CC_i, X) = CC_k$ endIf endFor <u>until</u> nothing more can be added to \mathbb{CC}

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6

Syntax Analysis - Part 3

```
SLR: Algorithm to Construct ACTION and GOTO Tables
Input: Grammar G, augmented with S' \rightarrow S
Output: ACTION and GOTO Tables
Construct "Canonical Collection of LR(0) items" along with MOVE function.
    \mathbb{CC} = \{ CC_0, CC_1, CC_2, CC_3, \dots CC_N \}
\underline{\mathtt{for}}\ \underline{\mathtt{each}}\ \mathrm{CC}_i\ \underline{\mathtt{do}}
  for each item in CC; do
     <u>if</u> the item has the form A \rightarrow \beta \cdot c \gamma
                           and MOVE (CC_i, c) = CC_i then
        set ACTION[i,c] to "Shift j"
     elseIf the item has the form A \rightarrow \beta • then
        for all b in FOLLOW(A) do
           set ACTION[i,b] to "Reduce A \rightarrow \beta"
     elseIf the item has the form S' \rightarrow S \cdot \underline{\text{then}}
        set ACTION[i, $] to "Accept"
  endFor
   for each nonterminal A do
     \underline{if} MOVE (CC<sub>i</sub>, \underline{A}) = CC<sub>i</sub> \underline{then}
        set GOTO[i,A] to j
     endIf
   endFor
endFor
```

YAPP

Yet Another PCAT Parser

An SLR Parser Generator

INPUT:

- A Grammar
- A String to Parse

ACTION:

- Build the parsing tables using the SLR algorithm
- Parse the string

YAPP is written in PCAT!

cs.pdx.edu/~harry/compilers/yapp

 ≈ 2100 lines of PCAT code.

Can be compiled by your compiler!!!

Example Input:

- A Grammar for PCAT (109 rules)
- String = the YAPP program itself

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69

Syntax Analysis - Part 3

Attributes in a Shift-Reduce Parser

An attribute can be associated with each grammar symbol.

$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0.t = \operatorname{Expr}_1.t + \operatorname{Term}.t;$

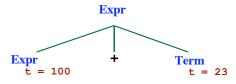
Attributes in a Shift-Reduce Parser

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$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0.t = \operatorname{Expr}_1.t + \operatorname{Term}.t;$

Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.



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7

Syntax Analysis - Part 3

Attributes in a Shift-Reduce Parser

An attribute can be associated with each grammar symbol.

$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0.t = \operatorname{Expr}_1.t + \operatorname{Term}.t;$

Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.



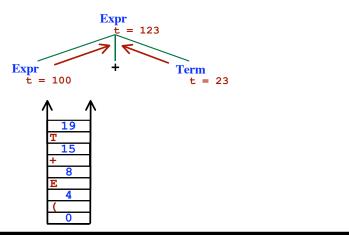
Attributes in a Shift-Reduce Parser

An attribute can be associated with each grammar symbol.

$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0 \cdot \mathsf{t} = \operatorname{Expr}_1 \cdot \mathsf{t} + \operatorname{Term} \cdot \mathsf{t};$

Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.



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73

Syntax Analysis - Part 3

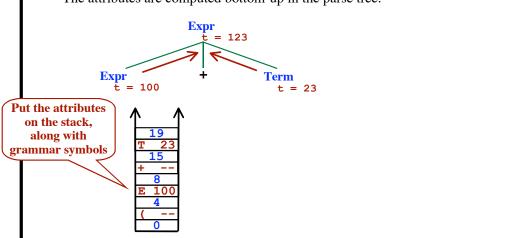
Attributes in a Shift-Reduce Parser

An attribute can be associated with each grammar symbol.

$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0 \cdot \mathsf{t} = \operatorname{Expr}_1 \cdot \mathsf{t} + \operatorname{Term} \cdot \mathsf{t};$

Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.



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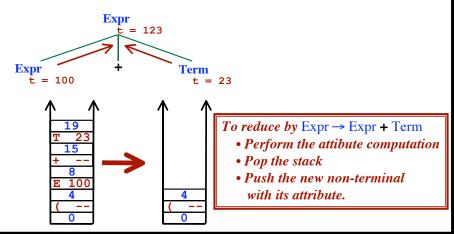
Attributes in a Shift-Reduce Parser

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$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
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Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.



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75

Syntax Analysis - Part 3

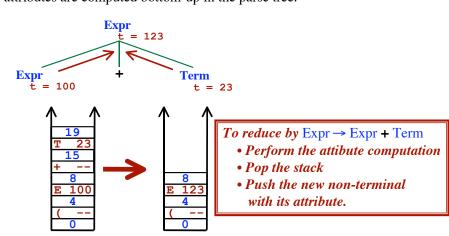
Attributes in a Shift-Reduce Parser

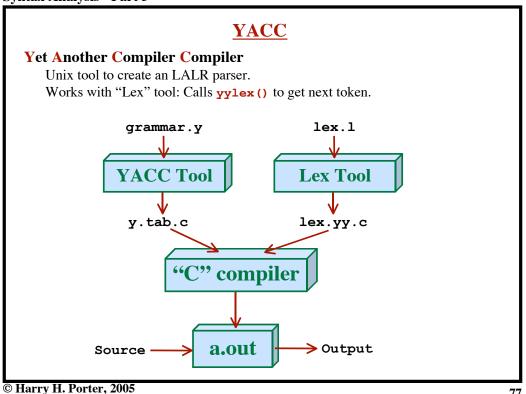
An attribute can be associated with each grammar symbol.

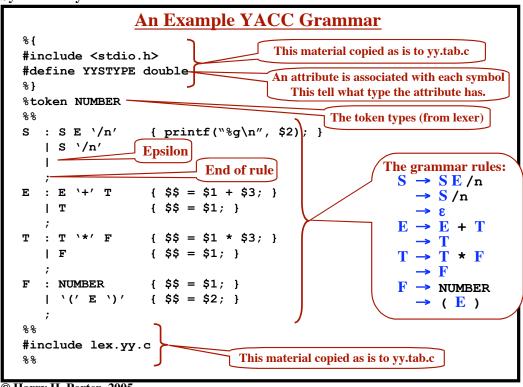
$$\operatorname{Expr}_0 \to \operatorname{Expr}_1 + \operatorname{Term}$$
 $\operatorname{Expr}_0 \cdot \mathsf{t} = \operatorname{Expr}_1 \cdot \mathsf{t} + \operatorname{Term} \cdot \mathsf{t};$

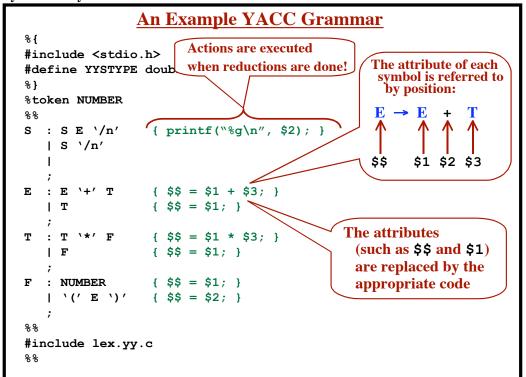
Synthesized Attributes:

The attributes are computed bottom-up in the parse tree.





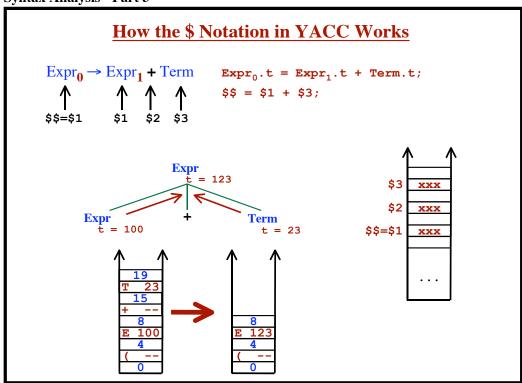




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70

Syntax Analysis - Part 3



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