

CS558 Programming Languages

Winter 2013

Lecture 2

IMPERATIVE LANGUAGES

Most commonly-used programming languages are **imperative**: they consist of a sequence of actions that alter the **state** of the world.

State includes the values of program variables and also the program's external environment (e.g. files the program reads or writes).

High-level imperative languages mimic the style of the underlying **Von Neumann** machine architecture, where programs are sequences of instructions that modify the contents of registers and memory locations.

This makes it relatively straightforward to compile imperative languages to efficient code:

- High-level variables are mapped to machine locations.
- High-level operations are mapped to (multiple) machine instructions.

Imperative languages are also natural for writing **reactive** programs that interact with the state of the “real world.” Examples:

- Reading mouse clicks and modifying the contents of a display.
- Controlling a set of relays in an external device.

STATEMENTS AND EXPRESSIONS

Many languages put have a separate syntactic category of **statements** (or **commands**) that includes stateful operations which don't produce a result value.

But in some languages, certain **expressions** can also affect the state (in which case they are said to have **side-effects**) in addition to returning a result.

Also, most languages support user-defined **functions**, which contain statements but return a value and are invoked in an expression context; this is another way expressions can have side-effects.

ASSIGNMENT

The basic primitive stateful operation is typically **assignment**, which alters a value stored in a **location**.

Depending on language, assignments are statements (with no result value), or expressions (maybe with result value).

In the simplest form, the location is associated with a simple **variable**, e.g.,

$$a := a + 2$$

(We use `:=` for assignment, `=` for equality relational operator. C/C++/Java use `=`, `==` respectively: a bad idea, because **both** form expressions.)

In most languages, the variable name `a` means different things on the left-hand and right-hand sides of an assignment.

On the LHS, `a` denotes the **location** of the variable `a`, into which the value of the RHS expression is to be stored.

On the RHS, `a` denotes the **value** currently contained in `a`, i.e., it indicates an implicit **dereference** operation.

OCAML REFERENCES

In OCaml, ordinary “variables” are **immutable**, i.e., they are really just names for values (computed at runtime), rather than for locations. Updatable variables, called **references**, must be explicitly created as such, and always serve as l-values. The contents of the variable must be **explicitly** dereferenced:

```
let x = ref 2 ;;  
x := !x + 2 ;;  
!x ;; (* yields 4 *)
```

```
let setto10 (y: int ref) = y := 10 ;;  
setto10 x ;;  
!x ;; (* yields 10 *)
```

This approach is somewhat more verbose, but removes any confusion between l-value and r-value.

INITIALIZATION VALUES

Most languages require variables (and other sources of l-values) to be **declared** before they are used: gives them a type and scope, and **optionally**, an initializing expression.

In fact, it is surely a **bug** to use any variable as an r-value unless it has previously assigned a value. But many languages permit us to write such code, resulting in runtime errors—either checked (as in Python) or unchecked (as in C).

The simplest fix is to **require** an initial value to be given for every declared variable. OCaml requires this for mutable `ref` variables (and also of course for ordinary immutable variables).

Java takes a slightly more sophisticated approach:

- variables do not need to be initialized at the point of declaration; but
- they **must** be initialized before they are actually used.

But in any reasonably powerful language, checking initialization before use is an **uncomputable** problem.

DEFINITE ASSIGNMENT

So the Java language reference manual carefully details a **conservative**, computable, set of conditions, which every program must meet, that guarantee there will be no uses before definition.

This is called the **definite assignment** property; just defining it takes 16 pages of the reference manual.

Some programs that **do** in fact initialize before use will be rejected because they violate the conditions.

Legal example:

```
int a;
if (b) /* b is boolean */
    a = 3;
else
    a = 4;
a = a + 1;
```

Illegal example:

```
int a;
if (b)
    a = 3;
if (!b)
    a = 4;
a = a + 1;
```

ORDER OF EVALUATION

Order of stateful operations affects program semantics (behavior).

Statements are always explicitly ordered, making these differences obvious.

Expressions can also have side-effects, but order of evaluation is often **under-specified** (precedence and associativity don't always fix order).

ANSI C example:

```
a = 0;  
b = (a = a + 1) - (a = a + 2);
```

Result ($1-3 = -2$ or $3-2 = 1$?) depends on compiler whim.

HIDDEN SIDE EFFECTS

Side-effects are not always obvious:

```
int a = 0;
int h (int x, int y) { return x; }
int f (int z) { a = z; return 0; }
h(a,f(2)); // = 0 or 2 ??
```

Keeping expression evaluation order or argument evaluation order undefined sometimes lets compiler generate more efficient code.

But most modern languages (e.g., Java) have moved towards precise definition of evaluation order within expressions (typically left-to-right).

STRUCTURED CONTROL FLOW

All modern higher-level imperative languages are designed to support **structured programming**.

Loosely, a structured program is one in which the **syntactic structure** of the program text corresponds to the **flow of control** through the dynamically executing program.

Originally proposed (most famously by Dijkstra) as an improvement on the incomprehensible “spaghetti code” that is easy to produce using the labels and jumps supported directly by hardware.

More specifically, structured programs use a very small collection of (recursively defined) **compound statements** to describe their control flow.

KINDS OF COMPOUND STATEMENTS

- Sequential composition: form a statement from a sequence of statements, e.g.

(Java) { x = 2; y = x + 4; }

(Pascal) begin x := 2; y := x + 4; end

- Selection: execute one of several statements, e.g.,

(Java) if (x < 0) y = x + 1; else z = y + 2;

- Iteration: repeatedly execute a statement, e.g.,

(Java) while (x > 10) output(x--);

(Pascal) for x := 1 to 12 do output(x*2);

SELECTION: IF

The basic selection statement is based on boolean values

```
if  $e$  then  $s_1$  else  $s_2$ 
```

which translates to

```
    evaluate  $e$  into  $t$   
    cmp  $t$ , true  
    brneq  $l_1$   
     $s_1$   
    br  $l_2$   
 $l_1$ :     $s_2$   
 $l_2$ :
```

SELECTION: CASE

To test types with more than two values, multi-way selections against constants are appropriate:

```
case  $e$  of
   $c_1$  :  $s_1$ 
   $c_2$  :  $s_2$ 
  ...
   $c_n$  :  $s_n$ 
default :  $s_d$ 
```

The most efficient translation of `case` statements depends on **density** of the value c_1, c_2, \dots, c_n within the range of possible values for e .

SPARSE CASES

For **sparse** distributions, it's best to translate the case just as if it were:

```
t := e;  
if t = c1 then  
    s1  
else if t = c2 then  
    s2  
else  
    ...  
else if t = cn then  
    sn  
else  
    sd
```

DENSE CASES

For a **dense** set of labels in the range $[c_1, c_n]$, it's better to use a **jump table**:

```

    evaluate e into t
    cmp t, c1
    brlt ld
    cmp t, cn
    brgt ld
    sub t, c1, t
    add table, t, t
    br *t
table: l1
        l2
        ...
        ln
l1:   s1
        br done
l2:   s2
        br done
        ...
ln:   sn
        br done
ld:   sd
done:
```

The best approach for a given case may involve a combination of these two techniques. Compilers differ widely in the quality of the code generated for case.

The basic loop construct is

```
while  $e$  do  $s$ 
```

corresponding to:

```
top:  evaluate e into t  
      cmp  $t$ , true  
      brneq done  
       $s$   
      br top  
done:
```

A commonly-supported variant is to move the test to the bottom:

```
repeat  $s$  until  $e$ 
```

which is equivalent to:

```
 $s$ ;  
while not  $e$  do  $s$ 
```


LOOP EXITS

It is sometimes desirable to exit from the middle of a loop:

```
loop
  s1;
  exitif e;
  s2
end
```

is equivalent to:

```
top: s1
    evaluate e into t
    cmp t,true
    breq done
    s2
    br top
done:
```

C/C++/Java have an unconditional form of `exit`, called `break`. They also have a `continue` statement that jumps back to the top of the loop.

USES FOR goto?

An efficient program with goto:

```
int i;
for (i = 0; i < n; i++)
    if (a[i] == k)
        goto found;
n++;
a[i] = k;
b[i] = 0;
found:
b[i]++;
```

In most languages (e.g., Modula, C/C++) there is **no** equivalently efficient solution without goto.

MULTI-LEVEL break

But we **can** do as well in Java, using a named, multi-level break:

```
int i;
search:
{ for (i = 0; i < n; i++)
    if (a[i] == k)
        break search;
    n++;
    a[i] = k;
    b[i] = 0;
}
b[i]++;
```

(This construct was invented by Knuth in the 1960's, but not adopted into a mainstream language for about 30 years!)

COUNTED LOOPS

Since iterating a definite number of times is very common, languages often offer a dedicated statement, with basic form:

```
for  $i := e_1$  to  $e_2$  do  $s$ 
```

Here s is executed repeatedly with i taking on the values $e_1, e_1 + 1, \dots, e_2$ in each successive iteration.

The detailed semantics of this statement vary, and can be tricky. Often, s is prohibited from modifying i , which (under certain other conditions) guarantees that the loop will be executed exactly $e_2 - e_1 + 1$ times.

C/C++/Java have a much more general version of `for`, which guarantees much less about the behavior of the loop:

```
for ( $e_1; e_2; e_3$ )  $s$ ;
```

is exactly equivalent to:

```
 $e_1$ ; while ( $e_2$ ) {  $s$ ;  $e_3$  }
```

ITERATORS

A number of modern languages support iteration over arbitrary sequences of values, not just sequences of numbers. For example, in Python we can write

```
for x in foo:
    # ...do something with x...
```

where `foo` is a list, string, tuple, dictionary, file, or in fact any object (including objects of user-defined classes) that has an `iter()` method.

We can write iterators using the `yield` statement to return values, e.g.

```
def my_iter():
    yield "foo"
    yield "bar"
    yield "baz"
```

```
for x in my_iter():
    print(x) # prints foo,bar,baz
```

Here the iterator and the consumer are acting as **coroutines**.

THE COME FROM STATEMENT

```
10 J = 1
11 COME FROM 20
12 PRINT J
   STOP
13 COME FROM 10
20 J = J + 2
```

(R. Lawrence Clark, “A linguistic contribution to GOTO-less programming,” *Datamation*, 19(12), 1973, 62-63.)

But is this really a joke?

Even with a GO TO, we must examine both the branch **and** the target label to understand the programmer’s intent.

INFORMAL SEMANTICS

- Grammars can be used to define the legal programs of a language, but not what they do! (Actually, most languages place further, non-grammatical restrictions on legal programs, e.g., type-correctness.)
- Language behavior is usually described, documented, and implemented on the basis of **natural-language** (e.g., English) descriptions.
- Descriptions are usually structured around the language's grammar, e.g., they describe what each nonterminal does.
- Natural-language descriptions tend to be **imprecise**, **incomplete**, and **inconsistent**.

EXAMPLE: FORTRAN DO-LOOPS

“DO n $i = m_1, m_2, m_3$

Repeat execution through statement n , beginning with $i = m_1$, incrementing by m_3 , while i is less than or equal to m_2 . If m_3 is omitted, it is assumed to be 1. m 's and i 's cannot be subscripted. m 's can be either integer numbers or integer variables; i is an integer variable.”

- from DEC Fortran-II manual, 1974.

Consider:

```
        DO 100 I = 10,9,1
...
100    CONTINUE
```

How many times is the body executed?

EXPERIMENTAL SEMANTICS

Try it and see!

Implementation becomes standard of correctness.

This is certainly **precise**: compiler source code becomes specification.

But it is:

- difficult to understand;
- awkward to use;
- subject to accidental change;
- wholly non-portable.

Aims:

- **Rigorous** and **unambiguous** definition in terms of a well-understood formalism, e.g., logic, naive set theory, etc.
- Independence from **implementation**. Definition should describe how the language behaves as abstractly as possible.

Uses:

- Provably-correct implementations.
- Provably-correct programs.
- Basis for language comparison.
- Basis for language design.

(But usually not basis for learning a language.)

Main varieties: **Operational, Denotational, Axiomatic.**

Each has different purposes and strengths. In this course, we'll mostly focus on operational semantics, with brief looks at the others.

OPERATIONAL SEMANTICS

Define behavior of language on an **abstract machine**.

Abstract machine should be much **simpler** than real machines, since otherwise a compiler for a real machine would be just as good!

Typical mechanisms:

- Characterize the state of the abstract machine (typically as an **environment** mapping variables to values) and give a set of **evaluation rules** describing how each syntactic construct affects the state.
- Define a simple Von Neumann-style **stack machine** and describe how each syntactic construct can be compiled into stack machine instructions.

Some useful things to do with an operational semantics:

- Build an implementation for a real machine by interpreting or compiling the abstract machine code.
- Explicate the meaning of a language feature by proving that it has the same behavior as a combination of simpler features.
- Prove that correctly typed programs cannot “dump core” at runtime.

SEMANTICS FROM INTERPRETERS

In the homework, we're building **definitional interpreters** for small languages that display key programming language constructs.

Our goal is to study the interpreter code in order to understand **implementation** issues associated with each language.

In addition, the interpreter serves as a form of **semantic** definition for each language construct. In effect, it defines the meaning of the language in terms of the semantics of Python or OCaml.

(Of course, you'll also be learning more about the semantics of Python and OCaml as we go!)

SEMANTICS AND ERRONEOUS PROGRAMS

An important part of a language specification is distinguishing valid from invalid programs.

It is useful to define three classes of errors that make programs invalid. (Of course, even valid programs may behave differently than the programmer intended!)

Static errors are violations of the language specification that can be detected at compilation time (or, in an interpreter, before interpretation begins)

- Includes: **lexical** errors, **syntactic** errors (caught during parsing), **type** errors, etc.
- Compiler or interpreter issues an error pinpointing erroneous location in source program.
- Language **semantics** are usually defined only for programs that have no static errors.

RUNTIME ERRORS

Checked runtime errors are violations that the language implementation is required to detect and report at runtime, in a clean way.

- Examples in Python, OCaml, or Java: division by zero, array bounds violations, dereferencing a null pointer.
- Depending on language, implementation may issue an error message and die, or raise an exception (which can be caught by the program).
- Language semantics must specify behavior precisely.

Unchecked runtime errors are violations that the implementation need not detect.

- Subsequent behavior of the computation is **arbitrary**. (Error is often not manifested until much later in execution.)
- Examples in C: division by zero, dereferencing a null pointer, array bounds violations.
- Language semantics probably don't specify behavior.
- **Safe** languages like Python, OCaml, and Java have **no** such errors!

AXIOMATIC SEMANTICS

Interpreters give an **operational** semantics for imperative statements.

(We'll see other, more formal, operational approaches to semantics later.)

An important alternative approach is to give a **logical** interpretation to statements.

- The **state** of an imperative program is defined by the values of the all its variables.
- We can characterize a state by giving a logical **predicate** (or **assertion**), mentioning the variables, which is **satisfied** by the values of the variables in that state.
- We can define the semantics of statements by saying how they affect (arbitrary) predicates.

TRIPLES INVOLVING ASSERTIONS

We write a **Hoare triple**

$$\{ P \} S \{ Q \}$$

to mean that if the **precondition** P is true before the execution of S then the **postcondition** Q will be true after the execution of S .

Note that the triple says nothing about what happens if S doesn't terminate. So we are only characterizing statements that terminate.

Examples of triples (not all stating true things!)

$$\{ y \geq 3 \} x := y + 1 \{ x \geq 4 \}$$

$$\{ x + y = c \} \text{ while } x > 0 \text{ do} \\ \quad y := y + 1; \\ \quad x := x - 1 \\ \text{end } \{ x + y = c \}$$

$$\{ y = 2 \} x := y + 1 \{ x = 4 \}$$

$$\{ y = 2 \} x := y + z \{ x = 4 \}$$

AXIOMS AND RULES OF INFERENCE

How do we distinguish true triples from false?

Who's to say which ones are true?

It all depends on the **semantics** of statements!

If we work in a suitably structured language, we can give a fixed set of **axioms** and **rules of inference**, one for each kind of statement. We then take as true the set of triples that can be logically **deduced** from these axioms and rules.

Of course, we want to choose axioms and rules that capture our intuitive understanding of what the statements do, and they need to be as **strong** as possible.

ASSIGNMENT AXIOM

$$\{ P[E/x] \} \ x := E \ \{ P \}$$

where $P[E/x]$ means P with all instances of x replaced by E .

This axiom may seem backwards at first, but it makes sense if we start from the postcondition. For example, if we want to show $x \geq 4$ after the execution of

$$x := y + 1$$

then the necessary precondition is $y + 1 \geq 4$, i.e., $y \geq 3$.

MORE RULES FOR STATEMENTS

Conditional Rule

$$\frac{\{ P \wedge E \} S_1 \{ Q \}, \{ P \wedge \neg E \} S_2 \{ Q \}}{\{ P \} \text{ if } E \text{ then } S_1 \text{ else } S_2 \text{ endif } \{ Q \}}$$

Composition Rule

$$\frac{\{ P \} S_1 \{ Q \}, \{ Q \} S_2 \{ R \}}{\{ P \} S_1; S_2 \{ R \}}$$

While Rule

$$\frac{\{ P \wedge E \} S \{ P \}}{\{ P \} \text{ while } E \text{ do } S \{ P \wedge \neg E \}}$$

BOOKKEEPING RULES

Consequence Rule

$$\frac{P \Rightarrow P', \{ P' \} \text{ S } \{ Q' \}, Q' \Rightarrow Q}{\{ P \} \text{ S } \{ Q \}}$$

Here $P \Rightarrow Q$ means that “ P implies Q ,” i.e., “ Q is true whenever P is true,” i.e. “ P is false or Q is true.” Hence we always have $\text{False} \Rightarrow Q$ for **any** Q !

PROOF TREE EXAMPLE

<p>----- (ASSIGN)</p> $\{x + y + 1 = c + 1\}$ $y := y+1$ $\{x + y = c + 1\}$ <p>----- (CONSEQ)</p> $\{x + y = c \wedge x > 0\}$ $y := y+1$ $\{x + y = c + 1\}$	<p>----- (ASSIGN)</p> $\{x - 1 + y = c\}$ $x := x-1$ $\{x + y = c\}$ <p>----- (CONSEQ)</p> $\{x + y = c + 1\}$ $x := x-1$ $\{x + y = c\}$
----- (COMP)	
$\{x + y = c \wedge x > 0\}$ $y := y+1; x := x-1$ $\{x + y = c\}$	
----- (WHILE)	
$\{x + y = c\}$ $\text{while } x > 0 \text{ do } y := y+1; x := x-1 \text{ end}$ $\{x + y = c \wedge \neg x > 0\}$	
----- (CONSEQ)	
$\{x + y = c\}$ $\text{while } x > 0 \text{ do } y := y+1; x := x-1 \text{ end}$ $\{x + y = c\}$	

ANNOTATED PROGRAM EXAMPLE

Proof trees can be unwieldy. Because the structure of the tree corresponds directly to the structure of the program code, it is common to use an alternative representation of proofs in which we annotate programs with assertions.

```
{x + y = c}
while x > 0 do
  {x + y = c ∧ x > 0}
  {x + y + 1 = c + 1}
  y := y + 1;
  {x + y = c + 1}
  {x - 1 + y = c}
  x := x - 1
  {x + y = c}
end
{x + y = c ∧ ¬ x > 0}
{x + y = c}
```

To verify that this is a valid proof, we have to check that the annotations are consistent with each other and with the rules and axioms.

MERITS AND PROBLEMS OF AXIOMATIC SEMANTICS

Gives a very clean semantics for structured statements.

But things get more complicated if we add features like:

- expressions with side-effects
- statements that break out of loops
- procedures
- non-trivial data structures and aliases

Useful for formal proofs of program properties (though these are seldom done).

Thinking in terms of assertions is good for **informal** reasoning about programs. (And there are beginning to be useful automated theorem proving support tools too.)

Other forms of semantic definition, e.g., **natural semantics**, also use similar **logical** structures.