## CS581 Worksheet \# 7

Due by midnight, Thursday, May 16th, Submit via D2L

1. Let $B$ be the set of all infinite sequences over $\{0,1\}$. Show that $B$ is uncountable, by using a diagonalization argument.
2. Let $\mathrm{A}_{\varepsilon C F G}=\{\langle\mathrm{G}\rangle \mid \mathrm{G}$ is a CFG that generates $\varepsilon\}$. Show that is decideable.
3. Let $X$ be the set $\{1,2,3,4,5\}$ and $Y$ be the set $\{6,7,8,9,10\}$. We describe the functions $\mathrm{x}: \mathrm{X} \rightarrow \mathrm{Y}$, and $\mathrm{g}: \mathrm{X} \rightarrow \mathrm{Y}$ in the following tables. Answer each part and give a reason why if the answer is negative.
4. Is $f$ one-to-one?
5. Is fonto?
6. Is facorrespondance?
7. Is g one-to-one?
8. Is g onto?
9. Is g a correspondance?

| $n$ | $f(n)$ |
| :--- | :--- |
| 1 | 6 |
| 2 | 7 |
| 3 | 6 |
| 4 | 7 |
| 5 | 6 |


| $n$ | $g(n)$ |
| :--- | :--- |
| 1 | 10 |
| 2 | 9 |
| 3 | 8 |
| 4 | 7 |
| 5 | 6 |

